273126 $^{58 PPs}$

NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

WARTIME REPORT

ORIGINALLY ISSUED
May 1944 as
Advance Restricted Report 4E31

TORSION TESTS OF STIFFENED CIRCULAR CYLINDERS

By R. L. Moore and C. Wescoat
Aluminum Company of America

NACA

WASHINGTON

58p

NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

ADVANCE RESTRICTED REPORT

TORSION TESTS OF STIFFENED CIRCULAR CYLINDERS

By R. L. Moore and C. Wescoat

INTRODUCTION

The design of curved sheet panels to resist shear involves a consideration of several factors: the buckling resistance of the sheet, the stress at which buckling becomes permanent, and the strength which may be developed beyond the buckling limit by tension-field action. Although some experimental as well as theoretical work has been done on the buckling and tension-field phases of this problem, neither of these types of action appears to be very well understood. The problem is of sufficient importance from the standpoint of aircraft design, it is believed, to warrant further experimental investigation. This report presents the results of the first series of torsion tests of stiffened circular cylinders to be completed in connection with this study at Aluminum Research Laboratories.

In some respects the shear problem for curved sheet panels is similar to that for flat panels. The buckling resistance depends not only upon curvature and the proportions of panel but also upon the restraint provided at the edges The strength which may be developed byyond the buckling limit depends upon the capacity of the sheet to transmit shear by diagonal tension and the resistance of the stiffener system to such tensile forces. The suddenness with which buckling generally occurs in a curved sheet would appear to make this action more determinate by experimental methods than is the case in flat sheet where the effects of eccentricities of loading usually obscure well-defined buckling phenomena. Tension-field action is more complex for curved panels, however, in that the stiffeners are subjected to combined bending and twist as well as axial compression.

Several solutions have been proposed for the problem of elastic shear-buckling in curved sheet panels. The ANC-5 Handbook (reference 1) indicates that this property may be determined by computing the critical stress for a flat panel of the same proportions and adding a factor depending upon curvature. This solution is similar in form to that proposed by Wagner and Ballerstedt (reference 2). Kromm (reference 3) has derived an approximate formula for the stability limit of infinitely long curved plate strips; while Ebner (reference 4) indicates that this property may be determined by formulas similar to those developed for curved panels under compression. Schapitz (reference 5) concludes that the shear-buckling action of curved sheet is largely unexplained. The latter reference presents the results of torsion tests of three stiffened circular cylinders and gives an analysis of tension-field action. Emphasis is placed upon the need for additional tests, not only to indicate shear-buckling characteristics, but to show the buckle patterns and stresses accompanying tension-field action.

OBJECT

The object of this investigation was to obtain, by means of torsion tests of stiffened circular cylinders, information on the behavior of curved sheet panels in shear. Four types of action have been considered:

(1) The shear-buckling resistance of cylinders having ring stiffeners only, for which the buckling limit is also the ultimate strength.

(2) The shear-buckling resistance of panels of cylinders having both longitudinal and ring stiffeners.

(3) The shear strength attainable beyond the buckling limit through the development of tension-field action in cylinders having both ring and longitudinal stiffeners.

(4) The permanent buckling characteristics of curved panels.

SPECIMENS

The specimens for these tests were circular cylinders, formed of 0.020- by 36- by 96-inch 24S-T sheet. The mean diameter was 30.08 inches and the over-all length 36 inches. Figure 1 gives the essential structural details. The ring stiffeners were made of 1/2- by 1/2-inch 24S-T square bars, shaped cold to approximate size in forming rolls. After forming, the rings were spliced and machined to obtain the required diameter. The longitudinal stiffeners were formed of 0.032-inch 24S-T sheet. Figure 1 shows the nominal dimensions. One of these stiffeners was used at the longitudinal seam of all specimens in order to prevent the waviness which might otherwise occur in a long thin lap joint having a large number of closely spaced rivets. The end bulkhead rings were made from 3/8-inch-thick steel plates.

Shear-buckling characteristics within the elastic range were investigated for 10 different sizes of curved sheet panels the dimensions and specimen number designations of which are shown in figures 5 and 11. All sizes of panels were obtained by varying the stiffener spacings of four different cylinders. Specimens 14, 15, 20, and 21, having the closest spacings of stiffeners, were the only ones tested to failure involving tension-field action.

PROCEDURE

Method of Loading

Figure 2 shows the loading fixture in which the torsion tests were made. This equipment consists of two similar structural steel frames having a depth of 3 feet 6 inches at the center and an effective lever arm of 12 feet 1/8 inch. One frame was held against rotation by anchoring it to the floor by means of bolts used in floor inserts; the other was rotated by means of loading screws so arranged as to pull in opposite directions at the ends. Spherically seated nuts were provided at each end of both loading screws to accommodate the movement accompanying the expected angles of twist.

The forces at the ends of the movable frame were determined by means of an aluminum alloy dynamometer link having a capacity of 5000 pounds. This force, applied in opposite directions at the ends of the loading frame, provided a maximum torque capacity of about 60,000 foot-pounds. Calibration of the dynamometer indicated a linear relation between load and deflection throughout the entire working range (0.236-in. deflection for 5000-lb load). Deflections were estimated by means of a dial indicator to the nearest 0.0001 inch, corresponding to a torque of about 25 foot-pounds.

The application of torque required two operators, one at each of the loading screws. Since the center of rotation was not fixed, it was necessary to provide some means of keeping the two ends of the specimen in the same relative position, otherwise some transverse bending as well as torque might have been applied. Figure 3 shows the bar which was mounted on the longitudinal axis of the specimens to serve as a reference for maintaining the proper position relative to the floor. By keeping a dial indicator at the rotating end in a position where it could be viewed by one loading-screw operator during the application of torque, it was possible to keep the vertical position of the center of rotation constant within 0.001 or 0.002 inch. Readings were taken at intervals at the fixed end of the specimen until it was demonstrated that for practical purposes these movements were negligible.

Although torque was applied in increments in all tests, it was generally not practical to attempt to apply definite predetermined values. The zero reading for each case was obtained with the specimen suspended loosely between the loading frames in order to eliminate accidental and unknown clamping torques. After the specimen was bolted in place, the loading arm was rotated until a dynamometer reading approximately equal to that desired was obtained, after which a final adjustment for cylinder position was made.

When buckling torques were being determined, it was necessary to watch the dynamometer deflection readings closely in order to catch the maximum values since the torques fell off as soon as buckling occurred. It was generally not possible from visual observation to predict when this buckling action would occur. In the specimens having ring stiffeners only,* an increase in

*Longitudinal stiffener used at seam in all specimens not considered effective in increasing shear-buckling resistance.

the angle of twist after buckling only resulted in a further decrease in torque. If the angle of twist was returned to zero, however, a torque reading approximately equal to the initial buckling value was obtained when the sheet snapped back to its original curved form. In specimens having 8 or 16 longitudinal stiffeners as well as ring stiffeners, this sudden buckling action and subsequent falling off of the torque occurred repeatedly, although at gradually increasing values, until all panels were buckled.

The specimens having ring stiffeners only were subjected to more than one loading in an effort to obtain more representative buckling values. Tests were repeated in some instances with the specimen rotated 180° with respect to its original position or turned end for end. Loadings were also tried in several instances with a number of end-connection bolts removed to minimize strains resulting from clamping the end bulkheads tightly to the loading frames. Although a range of buckling values was obtained by this procedure, there was no evidence that the buckling action in one test influenced the behavior in subsequent loadings. Buckling usually occurred in the same part of the cylinder in each test, regardless of its position in the loading frames.

<center>Measurements</center>

In addition to visual observations of the behavior of the cylinders and the determination of buckling and ultimate torques, measurements of over-all twist, radial deflections, and strains were made.

The twists were determined by means of a 10-inch level bar, used in the manner indicated in figure 3. This instrument, equipped with a 45-second bubble and a micrometer screw graduated in 0.001 inch, was sensitive to changes in slope of about one part in fifty thousand. The reference bars for these measurements, which also served to support the reference used for maintaining vertical position, were located on the inside face of the end bulkheads. The effective length of specimen was assumed to be $35\frac{5}{8}$ inches, or the distance between bulkhead centers.

Radial deflections were determined by means of a dial gage graduated in 0.001 inch and mounted on a sliding

pivot on the reference bar located at the center of the
cylinders as shown in figure 3. This indicator could be
used to traverse the entire inside surface of the speci-
mens with the exception of a length of about 4 inches
at each end. Rings with setscrews were used on both
sides of the pivot to prevent sliding while readings at
any one section were being taken. The procedure followed
was to lay out a reference grid on one or more panels,
including the stiffeners along the edge, which would
provide sufficient data to indicate the progress and pat-
tern of the buckling action of the sheet and stiffeners.
Panels adjacent to the longitudinal seam of the specimens
were not considered suitable for this purpose, although
their action generally did not indicate any significantly
different behavior.

Strains in the sheet were measured by means of
Baldwin Southwark SR-4 type R-1 wire-resistance strain
rosettes. These rosettes were used in pairs, one gage
on each side of the sheet at each location. In some
cases an attempt was made to obtain an approximate meas-
ure of the strain distribution in a typical panel by
taking measurements at several different points as indi-
cated in figure 4. In others, rosettes were located at
the centers of panels only. These gages were attached
by means of Duco household cement after the surface of
the sheet had been roughened slightly with emery cloth
(Aloxite No. 320) and cleaned with acetone.

Strain measurements on the longitudinal stiffeners
were made by means of both SR-4 type A-1 wire-resistance
strain gages and a 10-inch Whittemore strain gage. The
Whittemore strain gage was more suited for measurements
of extreme fiber stresses, although the gage length was
too long in most cases to be sensitive to variations in
bending along the length of the stiffeners. The wire
strain gages were too wide to be cemented to the curved
flanges of the longitudinal stiffeners and hence could
be placed only on the sides where they were relatively
insensitive to bending. A few strain measurements were
taken on the ring stiffeners in the first tests by means
of wire gages, but these determinations were not con-
tinued on all specimens.

Figure 4 shows the instrumentation used in the de-
termination of strains by means of the wire-resistance
gages. Unit strains were read directly in microinches
by means of the Baldwin Southwark SR-4 strain indicator.

Computation of Stresses and Angles of Twist

Average shear stresses were computed from the relation

$$\tau = \frac{24T}{\pi D^2 t}$$

where

τ shear stress, psi

T torque, ft-lb

D mean diameter, in. (30.08)

and

t sheet thickness, in.

Angles of twist were computed from the relation

$$\theta = \frac{48TL}{\pi D^3 Gt}$$

where

θ over-all twist, radians

L length, in. $(35\frac{5}{8})$

and

G modulus of elasticity in shear, psi (3,950,000)

Measured strains were reduced to stresses using a modulus of elasticity of 10,500,000 psi and a Poisson's ratio of 1/3. The direction and the magnitude of the principal stresses in the sheet were determined from the rosette data by means of the usual biaxial stress relations.

The more complex formulas used for the computation of shear-buckling values and the stresses accompanying tension-field action are summarized in the appendix.

Auxiliary Tests of Stiffeners

Since the longitudinal stiffeners were formed sections, the actual dimensions differed slightly from the

nominal values indicated in figure 1. A representative
value for cross-sectional area was determined by weigh-
ing several samples of known length. Moments of inertia
about the principal axes and the location of the neutral
axis in bending were determined from strain and deflec-
tion measurements made in bending tests under central
concentrated loads. Compression tests also were made on
individual stiffener sections ranging from 3 to 36 inches
in length.

RESULTS AND DISCUSSION

Buckling of Cylinders Having Ring Stiffeners Only

Although numerous torsion tests of unstiffened cir-
cular cylinders have been reported (references 6 and 7),
the behavior of specimens of this type provides a logical
starting point for evaluating the effectiveness of stiff-
eners in increasing the shear-buckling resistance of
curved sheet. Figure 5 shows typical torque-twist curves
and indicates observed buckling ranges as well as theo-
retical buckling torques for different lengths of cylin-
drical section. The theoretical values were computed
according to reference 6, assuming hinged edges. Data
on measured wave lengths and angles of buckles are also
included. Figures 6 to 10 show the nature and the ex-
tent of the buckling action produced.

As indicated by the shape of the torque-twist
curves in figure 5, well-defined buckling values were
obtained in all cases. Repeated tests of the same speci-
men did not give identical values of buckling torque,
although the differences obtained were not large. Mini-
mum torques in any one series of tests ranged from 83
to 98 percent of the maximum. Within the range of shear-
resistant action before buckling, the torsional stiff-
ness was in good agreement with that computed.

The maximum depths of buckles shown in figures 6
to 10 range from about 3/16 inch for the closest spacing
of ring stiffeners to about 5/8 inch for the widest
spacing. The fact that buckles of this depth could be
produced repeatedly without any consistent or appreciable
difference in the required torque indicates that the
action was essentially elastic. It should not be assumed
from these tests, however, that slight local permanent

sets are not a possibility at low shear-buckling stresses.
When a large buckle such as that shown in figure 6 is
formed rather violently, some part of the sheet may be
subjected to a sharp enough curvature to leave a notice-
able permanent crease, although the buckling resistance
in subsequent tests may not be materially affected. Such
an observation was made in the case of specimen 16 for
a shear stress of only about 1100 psi.

Table I shows that the average observed shear-
buckling stresses ranged from 77 to 93 percent of the
theoretical values based on reference 6, assuming hinged
edges. Some restraint was, of course, obtained at the
end bulkheads and the intermediate ring stiffeners; al-
though for the L/D ratios investigated, an assumption
of clamped edges would have increased the theoretical
buckling values only 10 to 12 percent. Part of the dis-
crepancy between observed and theoretical buckling
stresses undoubtedly may be attributed to local out-of-
roundness or initial buckles in the cylinders. The dif-
ference between the observed buckling values for specimens
13 and 13A indicates that a more uniform distribution of
shear stress and consequently a higher buckling value
may be obtained for interior panels than for panels ad-
jacent to the section of torque application. The ob-
served angles of buckling ranged from about 3° to 10°
greater than those computed according to reference 6,
the differences being greatest for the closest spacing
of ring stiffeners. The measured wave lengths were also
somewhat greater than were computed.

In general, the results of these tests are in fair
agreement with those reported by other investigators.
The experimentally determined buckling torques given in
reference 6 for cylinders without intermediate ring
stiffeners averaged about 75 percent of the theoretical
values for clamped edges with a minimum of 60 percent
of the theoretical; whereas the observed values for the
present tests averaged about 85 percent of the theoreti-
cal for hinged edges with a minimum in any one test of
70 percent of the theoretical. The method of computation
given in ANC-5 (reference 1) is quite conservative in
that it assumes that the minimum buckling resistance to
be expected for average cylinders of the proportions con-
sidered will not exceed about 60 percent of the theo-
retical.

Buckling of Curved Panels

Figures 11 and 16 show the torque-twist curves and
the buckling ranges or values observed for 10 different
sizes of curved sheet panel. Although the torques for
first buckling were fairly well defined, all like panels
did not buckle simultaneously and it was necessary in
most cases to determine the ranges over which this ac-
tion occurred. The minimum buckling values for the
different sizes of panel shown in figure 11 ranged from
74 to 89 percent of the maximum values. For the speci-
mens having more than one spacing of ring stiffeners,
the buckling of the largest panels was the only action
definitely reflected by the torque-twist relations.
Buckling ranges or values for the smaller panels were
determined by visual observation.

Figures 12, 13, and 14 show the nature of the buck-
ling action obtained in the panels where radial deflec-
tions were measured. The angles of first buckling were
in every case slightly less than shown in figure 5 for
specimens having the same spacings of ring stiffeners
but without longitudinals, indicating that the longitudi-
nals had a significant effect upon the buckling charac-
teristics. The effect of the longitudinals probably
would have been more pronounced had the spacings not been
approximately equal to a multiple of the buckle wave
lengths obtained without these stiffeners.

Table II summarizes the mean observed shear-buckling
stresses for all sizes of panel and gives corresponding
computed values obtained by several methods. Ratios of
these observed to computed buckling stresses are given
in table III. Of principal interest from the standpoint
of design is the fact that the experimental buckling
values exceed those computed according to ANC-5
(reference 1) by as much as 30 to 130 percent. The
greatest differences are shown for the panels formed by
a close spacing of ring stiffeners. The ANC-5 values
were obtained by computing the buckling stresses for
flat panels having the same proportions as those tested
and adding a factor for curvature. Hinged edges were
assumed, although for all but the closest spacings of
ring stiffeners the assumption of partial or even com-
plete edge fixity would not have altered the results
appreciably.

The shear-buckling stresses computed according to references 3 and 4 are in much better agreement with observed values, although here again the greatest differences are shown for the closest spacings of ring stiffeners. The method of reference 3 was derived for infinitely long curved plate strips having simply supported edges. It was assumed that the buckling values for panels of the lengths considered were equal to the computed values for infinitely long panels multiplied by the ratio of the computed values for corresponding flat panels. In only two cases were the buckling values obtained by this procedure on the unsafe side. The method of reference 4 is more conservative and appears to offer a somewhat more practical basis for design. Failure to take proper account of edge restraining effects is probably partly responsible for its apparent shortcomings for close stiffener spacings. The importance of this factor is indicated by the fact that the theoretical buckling value for a 9 inch-long unstiffened cylindrical section of the proportions tested is only about 12 percent higher for fixed than for hinged edges; whereas for a 2-inch-long section the corresponding increase in buckling value is about 40 percent.

In the tests of the specimens having ring stiffeners only it will be recalled from table I that the observed buckling stresses averaged about 85 percent of the theoretical based on reference 6, assuming hinged edges. Table III shows that the mean observed buckling stresses for different lengths of cylindrical sections having 8 longitudinal stiffeners were from 92 to 106 percent of the theoretical values for the same lengths of unstiffened cylinders; whereas the buckling values for cylinders having 16 longitudinal stiffeners were from 26 to 56 percent greater than the theoretical for the corresponding unstiffened cylinders. Figure 15 illustrates these relations between shear-buckling stress, L/D ratio, and the number of longitudinal stiffeners. It appears from these tests that the buckling stress for an unstiffened cylinder may be increased about 20 percent by adding 8 equally spaced longitudinal stiffeners or increased about 60 percent by adding 16 equally spaced stiffeners.

Although the relative merits of different sizes of longitudinal stiffeners have not been investigated, the particular section chosen for these tests was adequate as far as buckling resistance was concerned in that it

remained essentially straight after buckling of the sheet
panels. How much smaller the stiffeners might have been
and still accomplish the same result is, of course, not
known. It is instructive to point out that as far as
the shear-buckling resistance of the panels was concerned,
the material in the stiffeners might have been used some-
what more effectively if it had been added uniformly to
the cylinder wall thickness. According to computations
the shear-buckling resistance would have been increased
about 40 percent by utilizing the material of 8 longi-
tudinals or 80 percent by utilizing that of 16 stiffeners.
These increases in buckling resistance are slightly
greater than obtained by the use of stiffeners.

Tension-Field Action

Tests to failure, involving the application of tor-
ques of from four to six times the values required to
produce first panel buckling, were made on only four
cylinders. Figure 16 shows complete torque-twist curves
for these specimens and indicates buckling ranges and
maximum torques.

The action of stiffened circular cylinders in the
tension-field range is so complex that no attempt has
been made from these few tests to formulate general
conclusions regarding such behavior. Some indication
of the principal elements of the problem may be obtained,
however, from a consideration of the torsional stiffness
after buckling, the buckle patterns and sheet stresses,
the stresses and deflections produced in the stiffeners,
and the ultimate torsional strengths.

Torsional stiffness. - The torque-twist curves in
figure 16 indicate four distinct stages in the behavior
of the cylinders: (1) the range of shear-resistant ac-
tion before buckling, for which the torsional stiffness
may be predicted closely on the assumption of pure
shear; (2) the buckling range, where there is a marked
decrease in the torsional stiffness as the sheet is being
stretched to where it is capable of transmitting shear
by diagonal tension; (3) the tension-field range in which
the shear in excess of the buckling value is carried
principally by tension in the sheet and an approximately
linear relation between torque and twist is again obtained;

and (4) ultimate failure, which may occur either by
fracture of the sheet or by collapse of some element of
the stiffener system.

Torsional stiffness in the range after buckling
appears to be dependent not only upon sheet thickness
and proportions of panel but also upon the properties
of the stiffeners. The use of two or more quite differ-
ent ring-stiffener spacings in all specimens except
specimen 15 made it impossible to evaluate the stiffness
of the different sizes of panels from measurements of
over-all twist only. Ratios of the rates of twist after
buckling to those before buckling were approximately as
follows:

Specimen 14 - 3.9
Specimen 15 - 4.1
Specimen 20 - 3.2
Specimen 21 - 2.8

The fact that specimen 21 was the stiffest in the tension-
field range is not surprising in view of the close spac-
ings of stiffeners, although an explanation for the
relative stiffnesses of specimens 14, 15, and 20 is not
apparent from inspection. The large decrease in tor-
sional stiffness after buckling is evidence of several
factors of importance in an analysis of tension-field
action: (1) the angle and distribution of the diagonal
tensile stresses in each panel, (2) the stretching of
the sheet between longitudinals from an arc to a posi-
tion approaching the chord, and (3) the radial deflec-
tions of the longitudinal and ring stiffeners.

Buckle patterns. - Figures 12, 13, and 14, previ-
ously referred to, illustrate the buckling characteris-
tics observed for torques covering the greater part of
the tension-field range investigated. The position and
angle of buckling, which it should be noted are not con-
stant with varying torques, are indicative of the paths
of the principal diagonal tensions. The torque-radial
deflection curves shown in figure 17 gives an indication
of the progress of this buckling. In those cases for
which the number of buckles and the location of the
points of maximum deflection remained fairly constant,
the curves indicate well-defined buckling action within
the range of critical torques selected. In those cases
where there was a shift in the buckle pattern, however,

the break or knee in the torque-deflection curves which
is indicative of buckling was less pronounced.

Sheet stresses. - Figures 18 to 21 show the torque
stress relations obtained from the strain rosette meas-
urements. In all cases the stresses given are the
averages of the measured values on the two sides of the
sheet. In general, the measured stresses before buckling
were reasonably consistent with those computed on the
assumption of pure shear. The diagonal tensions and
compressions were approximately equal to the agerage
shears and were inclined 45° to the longitudinal axis of
the specimens. The buckling torques indicated by these
stress determinations were within the ranges determined
from the twist measurements. After buckling, the diag-
onal tensions continued to vary linearly with torque
but their magnitudes increased to two or more times the
average shears and there was a marked shift in their
direction. The corresponding diagonal compressions
varied little in most cases from their values at the
buckling torques.

In view of the type of buckling shown in figures
12, 13, and 14, it was not expected that a very accurate
measure of the maximum sheet stresses accompanying
tension-field action could be obtained. In cases where
stresses were measured at more than one location in the
same panel, the values at the center were the highest.
An exception to this rule probably would have been
found had strain measurements been taken on specimen 19
(see buckle pattern in fig. 14). Local bending stresses,
which govern permanent buckling characteristics, were
obviously much higher than any of the average values
indicated but the locations and magnitudes of these
critical stresses were of course unknown.

The irregularities shown in certain of the torque-
stress relations for specimens 15 and 21, in the range
just after buckling, may apparently be attributed
largely to the effect of shifting buckle patterns. For
these cases, the computed angles of maximum tensions
ranged from about 45° before buckling, to values as low
as 13° after buckling. The fact that these angles were
not consistent with the wave angles shown in figure 12
suggests that the stresses measured were not the maxi-
mum tensions developed in the panels. In specimens 14
and 20, where there was less shift in the buckle patterns

relative to the strain rosettes, a better agreement be-
tween observed angles of buckling and computed angles of
maximum tensions was obtained.

Stiffener stresses and deflections. - Figures 22 to
25 indicate the manner and extent to which the stiffeners
participated in the development of tension-field action
after buckling. The relations between torque and average
compressive stress in the longitudinal stiffeners were
approximately linear. In general, the stresses indicated
by the wire resistance strain gages (13/16-in. gage
lengths) attached to the sides of the longitudinals were
in fair agreement with the averages of the extreme fiber
stresses determined by means of the 10-inch Whittemore
strain gage. Although the use of more than one ring--
stiffener spacing in all specimens except specimen 15
resulted in different degrees of tension-field action
in different panels and consequently variations in aver-
age compression along the lengths of the longitudinals,
it is believed that a fairly satisfactory measure of
the maximum compressive forces developed in these mem-
bers was obtained.

It is apparent from the measured radial deflec-
tions and the stress-distribution diagrams included in
figures 22 and 25 that the longitudinal stiffeners were
subjected to bending as well as to axial compression.
It was not possible from the measurements made, however,
to determine the maximum intensity of these bending
stresses. The location of the wire-resistance gages on
the sides of the stiffeners made them insensitive to
bending and the Whittemore readings gave only average
stresses over 10-inch gage lengths. The amount of in-
tegral action developed between the stiffeners and the
sheet to which they were attached was also an uncertain
factor.

Figure 22 gives the results of the few strain
measurements made on the ring stiffeners of specimen 14.
These stresses were not only small but appeared to be
influenced by local bending effects which could not be
fully evaluated. The observed radial deflections give
the most direct measure of the over-all action of the
ring stiffeners. These deflections, as well as those
of the longitudinal stiffeners, did not vary linearly
with torque but increased at an increasing rate as the
sheet was "stretched" between longitudinals. The greater

the departure of the sheet from its original curved form,
the greater the radial component of the sheet tension
acting on the stiffeners. The average compressive stresses
developed in the ring stiffeners may be estimated by as-
suming that the deflections were the result of a uniformly
distributed radial pressure, since there was no signifi-
cant difference between deflections measured at or midway
between longitudinals. The maximum deflection of 0.025
inch shown in figure 25 for the center stiffiner of speci-
men 21 corresponds to an average compressive stress of
about 17,800 psi.

Analysis of tension-field action. - Reference 5 indi-
cates the factors to be considered in an analysis of
tension-field action in stiffened circular cylinders and
gives formulas for computing the principal stresses in-
volved. It is apparent from an attempt to check the
behavior observed in these tests against that computed
by the proposed methods, however, that certain aspects
of the problem are still not well understood.

Table IV shows a comparison between measured sheet
and stiffener stresses and values computed on the assump-
tion of complete tension-field action. The angles of
principal tension used were assumed to coincide with the
observed angles of buckling. The fact that the ratios of
measured to computed stresses for the longitudinal stiff-
eners are less than unity indicates that partial rather
than complete tension-field action should have been as-
sumed. The majority of the ring stiffener stresses, how-
ever, exceed the computed values, the differences in the
case of specimen 21 being considerable. The maximum
measured sheet stresses are in fair agreement with those
computed.

As indicated in reference 5, the use of the rather
complex formulas proposed for incomplete tension-field
action requires the evaluation of several experimentally
determined factors. Except for the degree of tension-
field action indicated by the ratios of measured to com-
puted longitudinal stiffener stresses shown in table IV,
these tests have not contributed materially toward such
an evaluation. It may be shown that the angles of buck-
ling observed for the different panels are not consistent
with the so-called "wrinkling" factor for complete tension-
field action. Furthermore, the use of more than one
spacing of ring stiffeners in all specimens except 15
precluded the possibility of evaluating this factor from

measurements of over-all twist. Even in the case of
specimen 15, where a determination of this wrinkling
factor could be made, the computed angle of principal
tension was not in agreement with the angle of buckling
observed. Until considerably more data relating to
tension-field action in stiffened cylinders are availa-
ble, there appears to be little basis for making other
than the generally conservative assumption of complete
tension-field action.

Ultimate torsional strengths. - Table V gives the
average shear and the estimated maximum tensile and com-
pressive stresses developed in the four specimens loaded
to failure. In three cases failure occurred by collapse
of the longitudinal stiffeners as shown in figures 26, 28,
and 29; in the fourth the sheet fractured through the
connections to one of the end bulkheads as shown in fig-
ure 27. The fourth test was the one which indicated the
need for providing relatively high shear-resistant panels
adjacent to the end bulkheads to cushion tension-field
effects. The effectiveness of this procedure is indicated
by the fact that the average shear stress developed in
specimen 21 at failure was about 40 percent higher than
that developed in specimen 15, having the same stiffener
system except for the cushion panels at the ends.

The longitudinal stiffeners of specimens 14 and 21
collapsed at approximately the same estimated average
compressive stress, indicating that the length between
ring stiffeners rather than the number of longitudinals
was the controlling factor. The ring-stiffener spacing
at the center of specimen 20 was 50 percent greater than
in specimens 14 and 21, and consequently the longitudi-
nals collapsed at a lower stress. The buckling stresses
developed in the longitudinal stiffeners of these three
cylinders, for ring-stiffener spacings of 9 inches and
13.5 inches, were in close agreement with the stresses
developed by the same lengths of individual stiffener
section, tested as flat-end columns. Figure 30 shows a
comparison of these data. Failure in the column tests
occurred by twisting rather than by flexure, which ac-
counts for the considerable difference shown between the
test values and the computed Euler column curve.

Permanent sets. - Although no systematic effort to
determine relations between buckling and first permanent
set characteristics was made in these tests, some infor-
mation relating to this aspect of behavior was obtained.

The photographs in figures 26, 28, and 29 were taken
with considerable torque on the cylinders to emphasize
the buckle patterns. Except in the vicinity of the
longitudinal stiffeners which collapsed, the greater
part of these buckles in the sheet disappeared when the
torque was removed. Figure 27 shows practically no evi-
dence of permanent buckling in the center panels of
specimen 15 after the application of an average shear of
14,400 psi, accompanied by sheet deflections as high as
0.35 inch. The torque-twist curve shown for this speci-
men in figure 16, however, indicates considerable over-
all permanent set for a torque equal to only about 80
percent of the maximum. Measured deflections for speci-
men 14 indicated that depths of buckles of about 0.25
inch were produced by an average shear of 5100 psi with
no appreciable set, although subsequent loading of this
specimen showed a reduction in mean buckling value of
about 8 percent. It appears from these data that tests
to determine losses in buckling resistance may provide
a more sensitive measure of significant permanent set
than direct measurements of permanent sheet deflection.

SUMMARY AND CONCLUSIONS

The torsion tests of stiffened circular cylinders
described in this report are the first of a series to be
completed in an experimental investigation of the shear-
buckling resistance and strength of stiffened curved
sheet. Although a number of observations of interest
have been made regarding the behavior of this particular
group of 0.020-inch thick 24S-T cylinders, additional
tests are in progress which should be considered before
an attempt is made to formulate general conclusions. The
most significant results obtained thus far may be sum-
marized as follows:

1. The shear-buckling stresses observed for the cyl-
inders having ring stiffeners only averaged about 85 per-
cent of the theoretical values computed according to
Donnell, (reference 6), assuming hinged edges. This aver-
age is about 40 percent higher than the minimum to be
expected from average cylinders of these proportions,
according to ANC-5 (reference 1). Although the results
of these tests are in fair agreement with those previous-
ly reported, their value in this investigation lies in
the fact that they provide a basis for judging the rela-
tive effectiveness of longitudinal stiffeners in increas-
ing the shear-buckling resistance of curved sheet.

2. Table II gives mean observed shear-buckling stresses for 10 different sizes of curved sheet panels. These stresses were based on buckling phenomena which for the most part were well defined by the torque-twist relations shown in figures 11 and 16. Variations from the mean observed buckling value for any one size of panel did not exceed 15 percent.

3. The observed shear-buckling stresses given in table II are from 30 percent to 130 percent higher than computed according to ANC-5, assuming hinged edges. Computed values based on a modification of the solution given by Kromm (reference 3) for infinitely long curved panels, or upon the method proposed by Ebner (reference 4) are in much better agreement with test values. These methods should receive further consideration as a possible basis for design.

4. A comparison of the shear-buckling stresses observed for different lengths of cylindrical section, with and without longitudinal stiffeners, and the theoretical values for unstiffened sections indicates that the buckling resistance of a given cylinder may be increased about 20 percent by adding 8 equally spaced longitudinal stiffeners, or about 60 percent by adding 16 equally spaced longitudinals.

5. The results of the tests carried to ultimate failure permit a qualitative if not a very accurate quantitative analysis of the action involved in the tension-field range beyond buckling. Approximately linear relations were observed between torque and over-all twist for the greater part of the tension-field ranges, as shown in figure 16, although the rates of twist were three to four times those measured in the shear-resistant range before buckling. Linear relations were likewise observed between torque and average measured stresses in the sheet and longitudinal stiffeners, as shown in figures 18 to 25. The average compressive stresses in the ring stiffeners, based on measured radial deflections, and the bending stresses in the longitudinals showed a definite tendency to increase at a faster rate than the torques.

6. An analysis of tension-field action in stiffened circular cylinders subjected to twist involves a consideration of the buckling resistance of the sheet, the magnitude and direction of the principal tensile stresses produced in the sheet after buckling, the contraction of the sheet between longitudinals as a result of buckling,

and the size and spacing of the stiffeners. Schapitz
(reference 5) has indicated the manner in which these
factors may be recognized, but except for an assumed
case of complete tension-field action, his formulas re-
quire substitution of experimental constants not yet
evaluated.

7. Table IV gives a comparison between measured
sheet and stiffener stresses and values computed for
complete tension-field action according to Schapitz
(reference 5). The ratios of average measured to com-
puted stresses in the longitudinals indicate that incom-
plete rather than complete tension-field action should
have been assumed, although the results of the other
stress measurements are not generally consistent with
this observation.

8. Three of the four specimens loaded to the limit
of the tension-field range failed by collapse of the
longitudinal stiffeners. The average compressive
stresses developed for ring-stiffener spacings of 9 inches
and 13.5 inches were approximately the same as the
strengths developed by the same lengths of individual
stiffener sections tested as flat-end columns. The
fourth specimen failed by fracture of the sheet through
the connections to one end bulkhead.

9. Relations between average shear stresses and the
maximum deflections and bending stresses which may be
developed in sheet panels of different proportions after
buckling have not been sufficiently well defined to make
possible accurate predictions regarding permanent buck-
ling characteristics. If a structure can be loaded re-
peatedly without loss in buckling resistance, it can be
assumed, or course, that the action is elastic. Tests to
determine allowable load limits for elastic buckling
appear to provide a more sensitive measure of permanent
set than direct measurements of permanent sheet deflec-
tion.

Aluminum Research Laboratories,
    Aluminum Company of America,
        New Kensington, Pa., March 13, 1944.

APPENDIX

SUMMARY OF FORMULAS

Notation

τ shear-stress for applied torque, psi

τ_0 shear-buckling stress, psi

t sheet thickness, in.

D mean diameter, in.

r mean radius, in.

L length, in.

b arc length of panel, in.

a other dimension of panel, in.

σ maximum diagonal tension after buckling, psi

α angle of maximum diagonal tension, deg

σ_x average compression in longitudinal stiffeners, psi

σ_y average compression in ring stiffeners, psi

F_x area of longitudinal stiffener, sq in.

F_y area of ring stiffener, sq in.

E modulus of elasticity, psi, (10,500,000)

μ Poisson's ratio (1/3)

Reference 1 (ANC-5)

For unstiffened circular cylinders, where $\dfrac{L^2}{tD} > 20$

$$\tau_0 = K \frac{E}{\left(\dfrac{D}{t}\right)^{5/4}\left(\dfrac{L}{D}\right)^{1/2}}$$

where

K = 0.75 for hinged edges

For curved panels

$$\tau_0 = KE \left(\frac{t}{b}\right)^2 + K_1 E \frac{t}{r}$$

where

K   buckling factor for corresponding flat sheet
     panel depending on ratio of a/b

and

$K_1 = 0.1$

Reference 3 (Kromm)

For infinitely long curved plate strips having
hinged edges (central angle $\leqq 43^\circ$)

$$\tau_0 = 1.67 E \frac{t}{b} \sqrt{\frac{t}{r}}$$

when $\frac{b}{t} \sqrt{\frac{t}{r}} > 4.3$ (See reference 3 for other cases.)

For the panel lengths considered, values of τ_0 deter-
mined by the above relation were multiplied by the ratio
of the computed buckling stress for a flat panel of the
same proportions to that for an infinitely long flat
panel having the same short dimension.

Reference 4 (Ebner)

For curved panels

$$\tau_0 = \sqrt{\tau_R^2 + \left(\frac{\tau_P}{2}\right)^2} + \frac{\tau_P}{2}$$

where

τ_R shear-buckling stress for unstiffened cylinder

τ_P shear-buckling stress for corresponding flat panel

Reference 5 (Schapitz)

For complete tension-field action after buckling

$$\sigma = \frac{\tau}{\sin \alpha \cos \alpha} - \tau_0$$

$$\sigma_x = \frac{bt}{F_x} \ \tau_0 \ \left(\frac{\tau}{\tau_0} \cot \alpha - 1 \right)$$

$$\sigma_y = \frac{at}{F_y} \ \tau_0 \ \left(\frac{\tau}{\tau_0} \tan \alpha - 1 \right)$$

Reference 6 (Donnell)

For unstiffened circular cylinders having hinged ends where $\dfrac{L^2 t}{D^3} < 5.2$

$$\tau_0 = \frac{Et^2}{(1-\mu^2)L^2} \left[2.8 + \sqrt{2.6 + 1.4 \left(\sqrt{1-\mu^2} \ \frac{L^2}{tD} \right)^{3/2}} \right]$$

REFERENCES

1. Anon.: Strength of Aircraft Elements. Army-Navy-
       Civil Committee on Aircraft Design Criteria
       (ANC-5), 1942.

2. Wagner, H., and Ballerstedt, W.: Tension Fields in
       Originally Curved, Thin Sheets during Shearing
       Stresses. NACA TM No. 774, 1935.

3. Kromm, A.: The Limit of Stability of a Curved Plate
       Strip under Shear and Axial stresses. NACA TM
       No. 898, 1939.

4. Ebner, H.: The strength of Shell Bodies - Theory
       and Practice. NACA TM No. 838, 1937.

5. Schapitz, E.: The Twisting of Thin-Walled, Stiffened
       Circular Cylinders. NACA TM No. 878, 1938.

6. Donnell, L. H.: Stability of Thin-Walled Tubes
       under Torsion. NACA Rep. No. 479, 1933.

7. Lundquist, E. E.: Strength Tests on Thin-Walled
       Duralumin Cylinders in Torsion. NACA TN No. 427,
       1932.

TABLE I

TORSIONAL STRENGTHS OF 24S-T CYLINDERS HAVING RING STIFFENERS ONLY

Mean Diameter, D = 30.08 in.
Overall Length = 36 in.
Sheet Thickness = 0.020 in.

Specimen No.	Length of Buckled Section, L, in.†	L/D	Shear-Buckling Stresses, psi		
			Average Observed	Theoretical*	$\frac{\text{Observed}}{\text{Theoretical}}$
16	35.62	1.18	1 110	1 325	0.84
17	27.00	0.90	1 280	1 520	0.84
18	13.50	0.45	1 710	2 210	0.77
13	8.81	0.29	2 310	2 870	0.81
13A	9.00	0.30	2 570	2 770	0.93

† Center to center of ring stiffeners (See Fig. 5).

* Based on Reference 6, assuming hinged edges.

TABLE III

COMPARISON OF OBSERVED AND COMPUTED SHEAR-BUCKLING STRESSES FOR CURVED 24S-T SHEET PANELS GIVEN IN TABLE II

Specimen No.	Dimensions of Panels, in.	Ratio of Mean Observed to Computed Shear-Buckling Stresses Based On:			
		ANC-5	Ref. 3	Ref. 4	Ref. 6
	8 Longitudinal Stiffeners, 11.81 in. apart				
19	0.020 x 13.50 x 11.81	1.30	1.17	0.91	0.95
14	0.020 x 9.00 x 11.81	1.68	1.09	1.00	1.06
14	0.020 x 4.31 x 11.81	1.58	0.43	0.80	0.92
	16 Longitudinal Stiffeners, 5.90 in. Apart				
20	0.020 x 13.50 x 5.90	1.39	1.10	1.12	1.30
15	0.0195 x 8.81 x 5.90	1.60	-	-	1.26
15	0.0195 x 9.00 x 5.90	1.71	1.24	1.13	1.37
21	0.0205 x 9.00 x 5.90	1.84	-	-	1.42
21	0.0205 x 6.75 x 5.90	1.99	1.30	1.21	1.39
20	0.020 x 4.31 x 5.90	2.31	1.25	1.27	1.49
21	0.0205 x 2.06 x 5.90	2.02	0.71	1.50	1.56

TABLE V

TORSIONAL STRENGTHS OF 24S-T CYLINDERS HAVING BOTH RING AND LONGITUDINAL STIFFENERS

Mean Diameter = 30.08 in.
Overall Length = 36 in.

Specimen No.	Sheet Thickness, in.	Number of Longitudinal Stiffeners	Ring-Stiffener Spacing for Center Panels, in.	Maximum Torque, ft-lb	Stresses at Failure, psi			Location of Failure
					Average Shear	Maximum Tension in Sheet	Average Compression in Longitudinals	
14	0.020	8	9	28 600	12 100	33 500	34 000	Longitudinals
15	0.0195	16	9	33 200	14 400	35 000	20 000	Sheet
20	0.020	16	3.5	36 800	15 500	48 500	23 000	Longitudinals
21	0.0205	16	9	49 000	20 200	45 500	34 500	Longitudinals

W - 89

TABLE II

SHEAR-BUCKLING STRESSES FOR PANELS OF 24S-T CYLINDERS HAVING BOTH RING AND LONGITUDINAL STIFFENERS

Mean Diameter = 30.08 in.
Overall length = 36 in.

Specimen No.	Dimensions of Panels, in.	Mean Observed	Shear-Buckling Stresses, psi			
			Computed			
			ANC-5	Ref. 3	Ref. 4	Ref. 6*
	8 Longitudinal Stiffeners, 11.81 in. apart					
19	0.020 x 13.50 x 11.81	2 110	1 620	1 810	2 320	2 210
14	0.020 x 9.00 x 11.81	2 950	1 750	2 700	2 960	2 770
14	0.020 x 4.31 x 11.81	4 130	2 610	9 700	5 145	4 510
	16 Longitudinal Stiffeners, 5.90 in. apart					
20	0.020 x 13.50 x 5.90	2 870	2 070	2 600	2 570	2 210
15	0.0195 x 8.81 x 5.90	3 370	2 110	-	-	2 680
15	0.0195 x 9.00 x 5.90	3 590	2 100	2 880	3 170	2 680
21	0.0205 x 9.00 x 5.90	4 120	2 240	-	-	2 910
21	0.0205 x 6.75 x 5.90	4 740	2 380	3 650	3 900	3 400
20	0.020 x 4.31 x 5.90	6 750	2 920	5 400	5 300	4 510
21	0.0205 x 2.06 x 5.90	13 900	6 890	19 500	9 300	8 900

* Theoretical for cylinders having lengths equal to ring-stiffener spacings but without
longitudinals.

TABLE IV

COMPARISON OF MEASURED AND COMPUTED STRESSES WITHIN THE TENSION-FIELD RANGE
STIFFENED CIRCULAR 24S-T CYLINDERS

Specimen No.	Torque, ft-lb	Avg. Compression in Longitudinals, psi			Avg. Compression in Rings, psi			Maximum Tension in Sheet, psi		
		Measured*	Computed	Meas. Comp.	Measured+	Computed	Meas. Comp.	Measured**	Computed	Meas. Comp.
14	12 000	10 000	21 600	0.46	-	-	-	12 000	9 400	1.28
	20 900	22 500	35 000	0.64	1 400	2 000	0.70	22 000	16 400	1.34
	28 000	33 000	49 900	0.66	3 500	3 400	1.03	32 000	23 000	1.39
15	11 600	8 500	12 300	0.69	-	-	-	8 500	9 800	0.87
	20 000	12 000	17 400	0.69	2 100	1 100	1.91	15 000	16 100	0.93
	30 800	19 000	27 000	0.70	4 200	3 500	1.20	26 000	25 600	1.01
20	13 900	9 500	21 700	0.44	-	-	-	13 000	15 500	0.84
	22 200	14 000	33 100	0.42	-	1 000	-	24 000	23 800	1.01
	27 800	18 500	42 500	0.44	-	2 000	-	33 500	30 700	1.09
21	16 800	10 000	12 400	0.80	-	-	-	9 500	11 500	0.82
	22 200	14 000	16 900	0.83	2 800	1 400	2.00	14 500	16 000	0.91
	30 200	20 000	25 000	0.80	5 600	2 900	1.93	23 000	23 100	0.99
	41 600	29 000	37 300	0.78	17 500	5 100	3.44	36 500	33 400	1.09

All computed stresses based on Reference 5, assuming complete tension-field action.

* Based on average strains measured over 10-in. gage lengths near center of stiffeners.
** Based on average strains measured at centers of panels.
+ Based on measured radial deflections.

FIGURE 1.—
DETAILS OF STIFFENED CIRCULAR CYLINDERS
FOR TORSION TESTS

Fig. 2

Figure 2. – 60,000 ft/lb capacity torsion loading fixture.
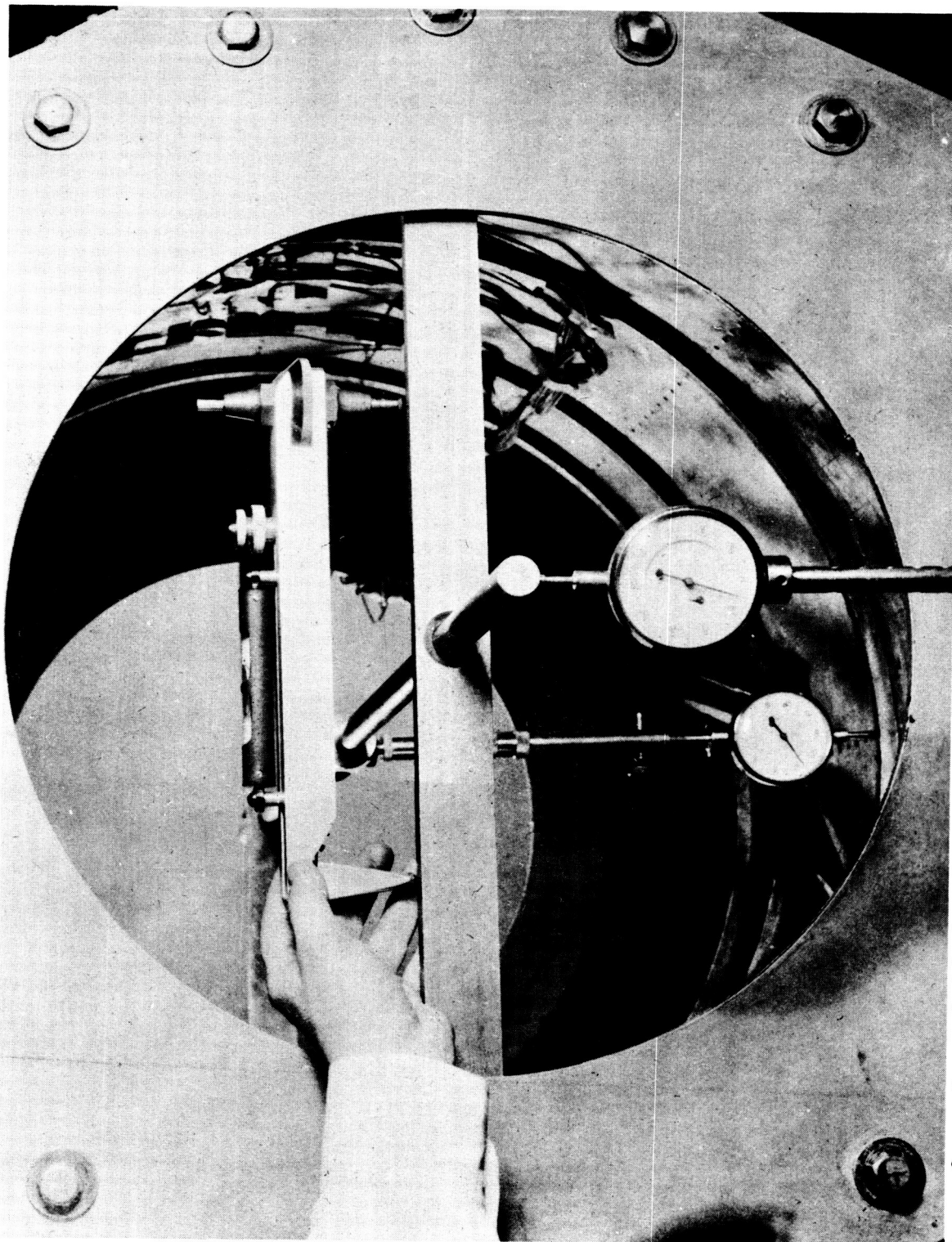
Figure 3. — Use of 10-in. level bar for measuring twist. Dial indicator inside cylinder used for measuring radial deflections. Dial indicator in foreground used to keep rotating end of cylinder in fixed position relative to the floor.
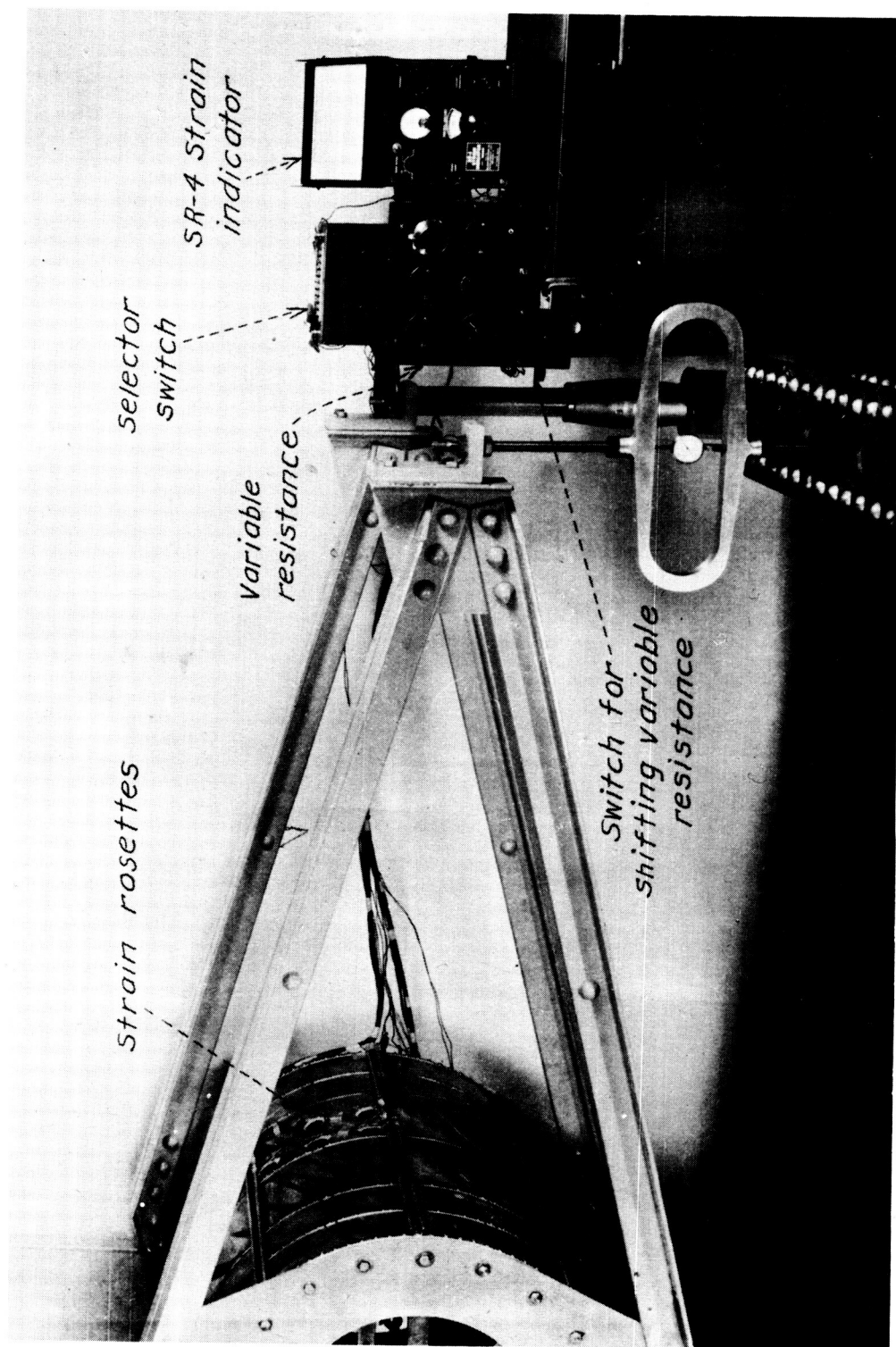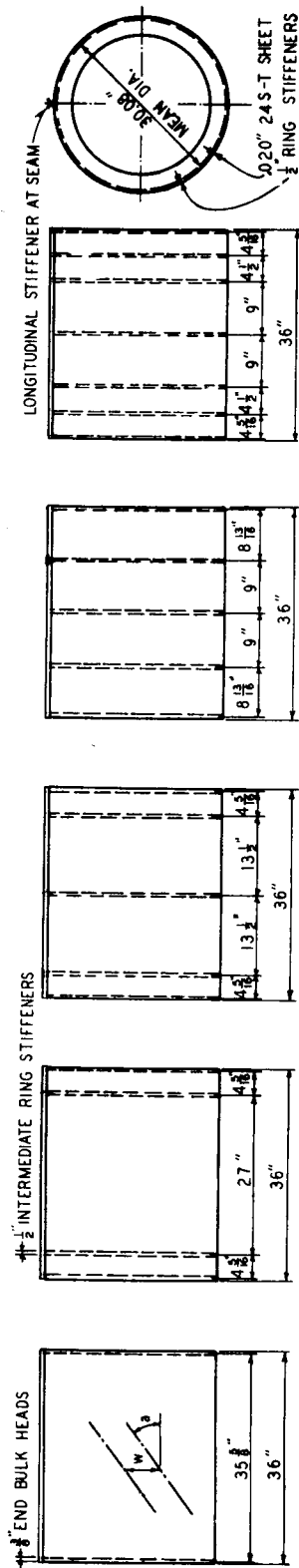
Figure 4. – Apparatus used in measuring strains by means of Baldwin Southwark SR-4 wire-resistance gages. Cylinder shown is specimen No. 14.

w-89.
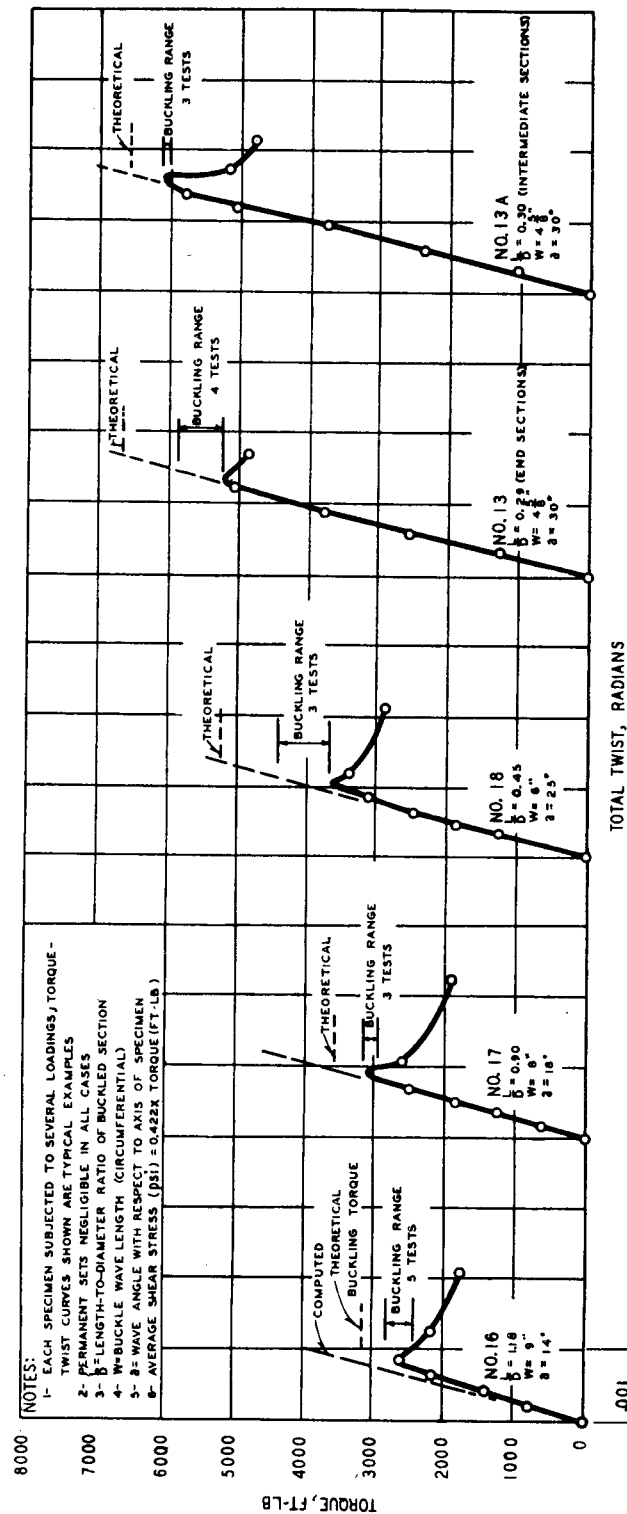
Figure 5   TORSIONAL STRENGTHS OF STIFFENED CIRCULAR CYLINDERS
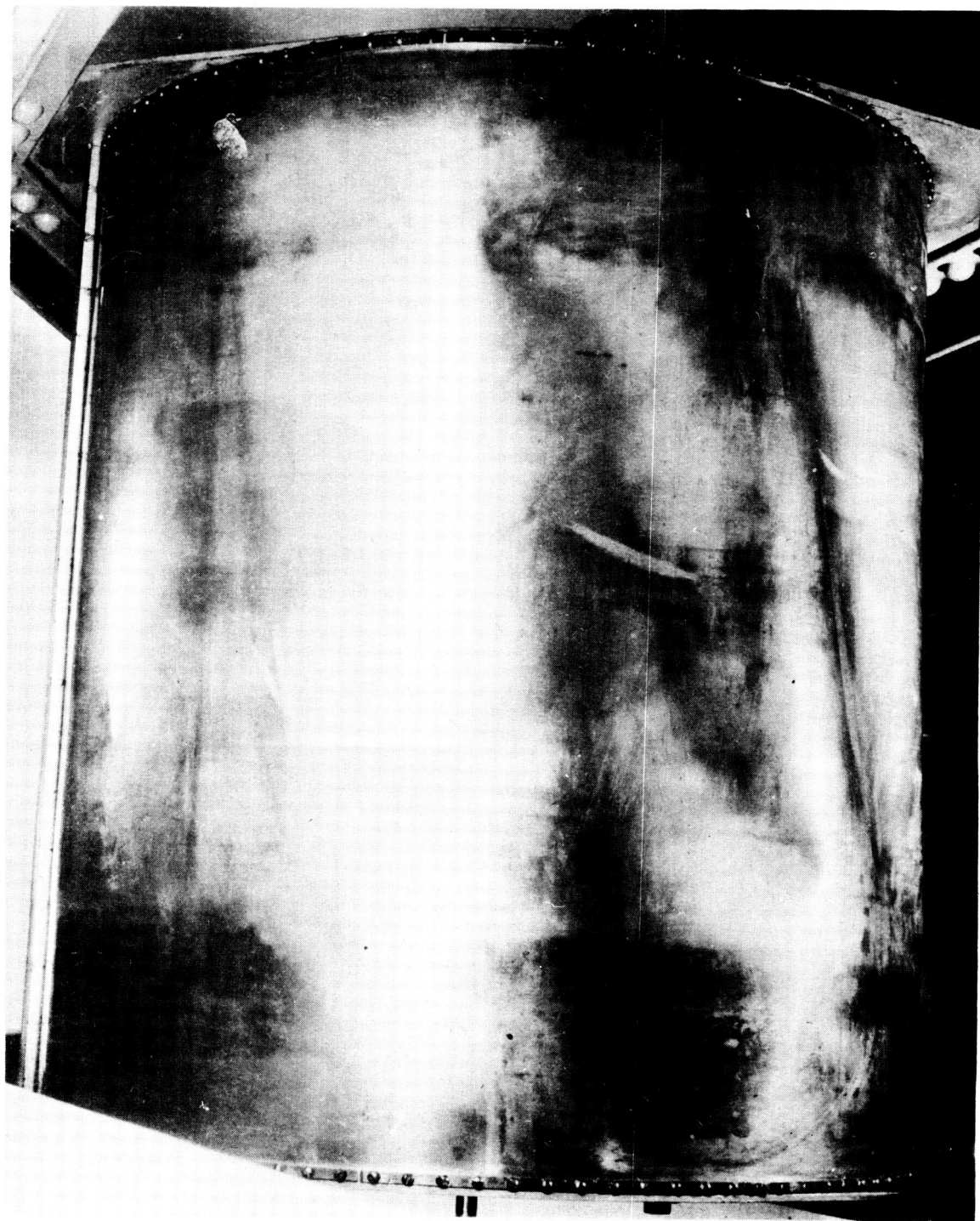
Figure 6. - Failure of specimen No. 16.
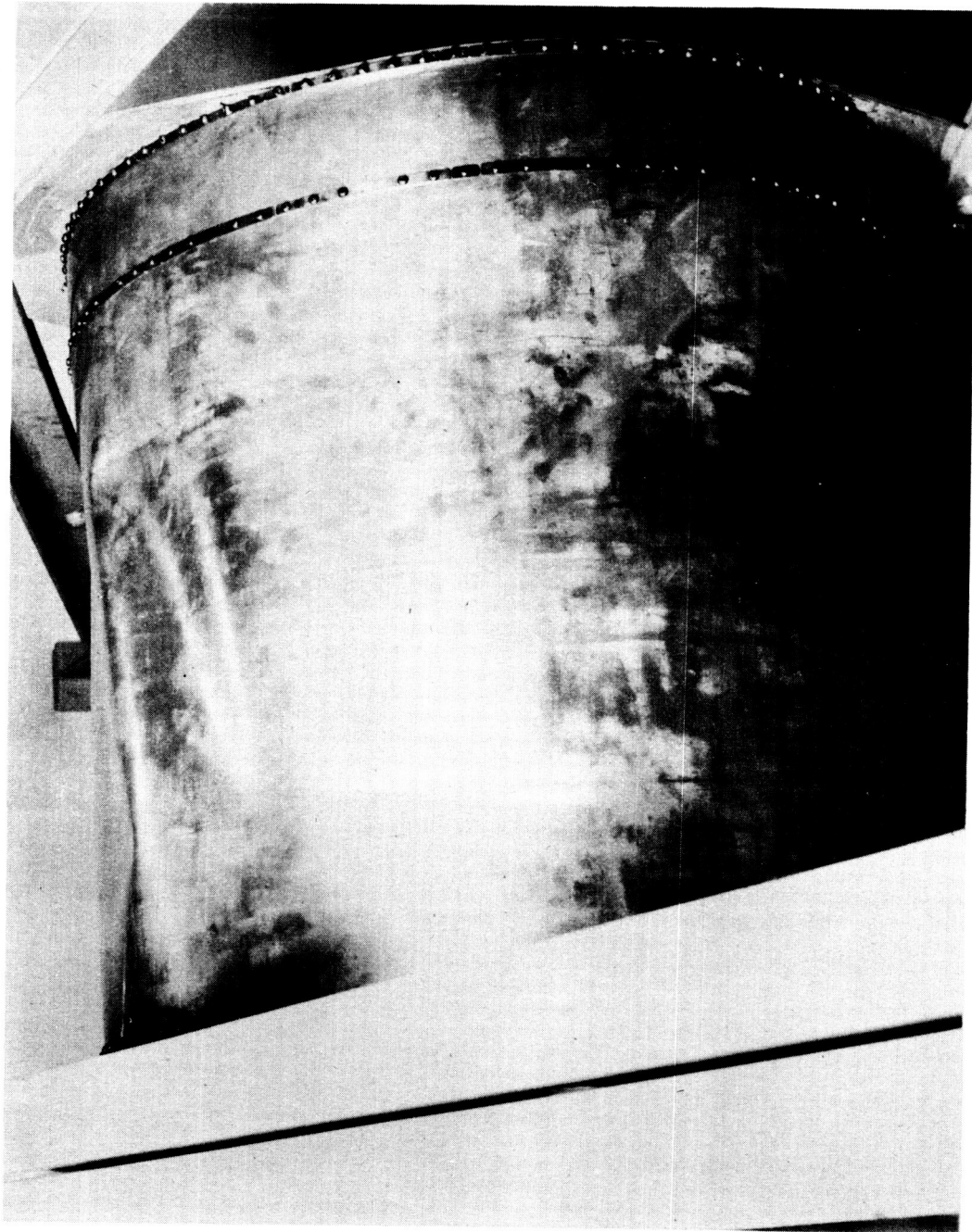
Figure 7. — Failure of specimen No. 17.

W-89
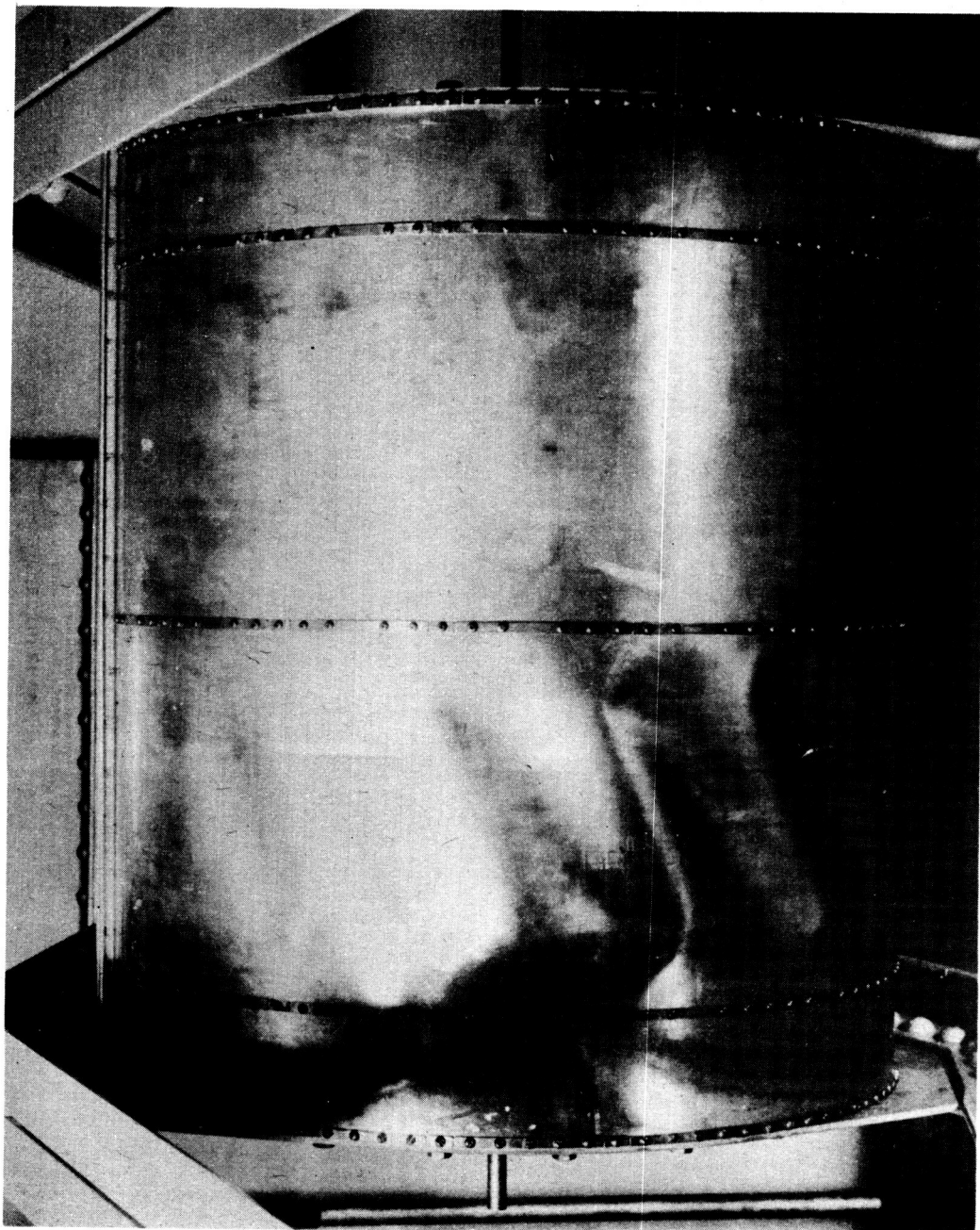
Figure 8. — Failure of specimen No. 18.
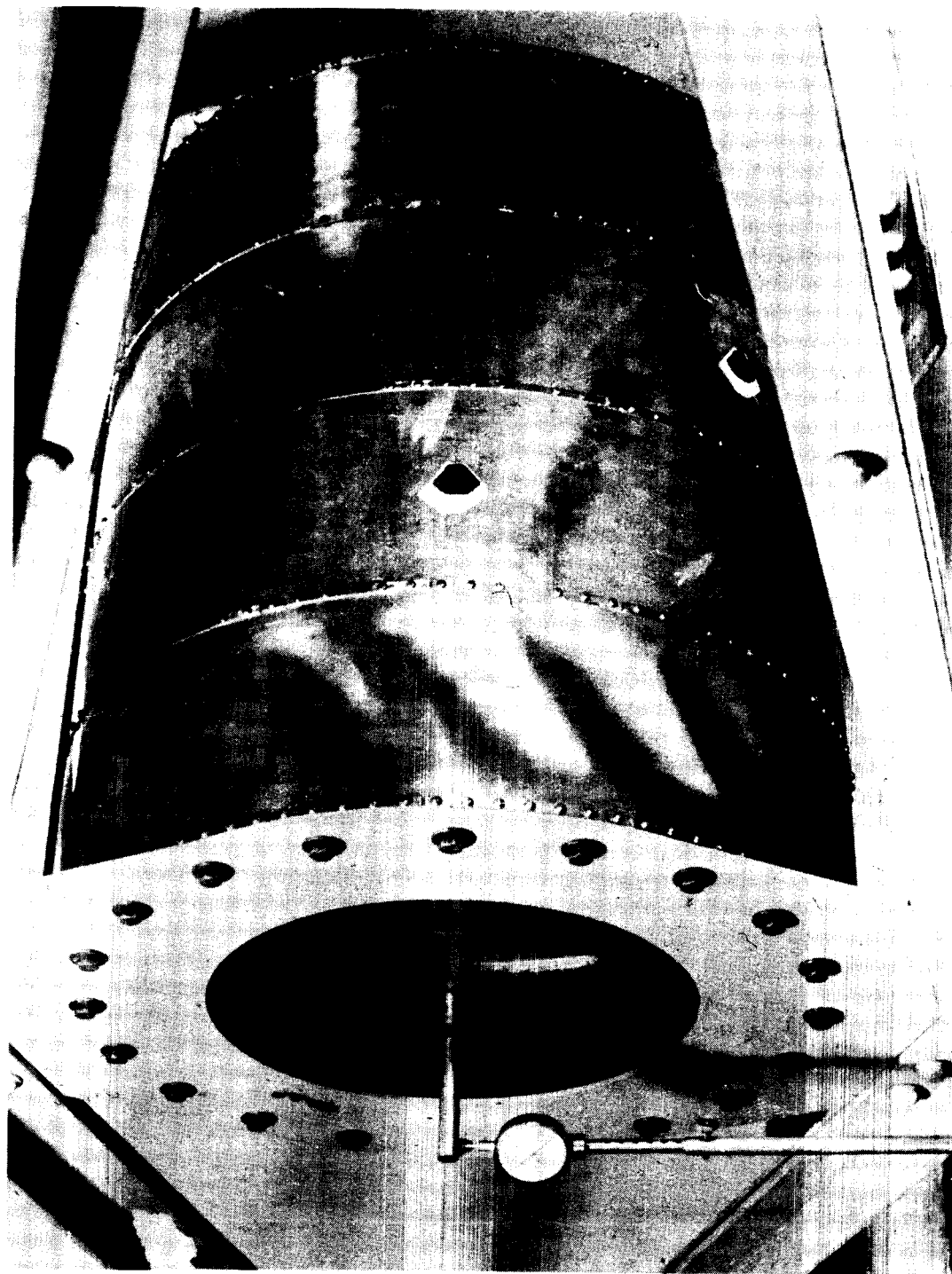
Figure 9. — Failure of specimen No. 13.

W-89
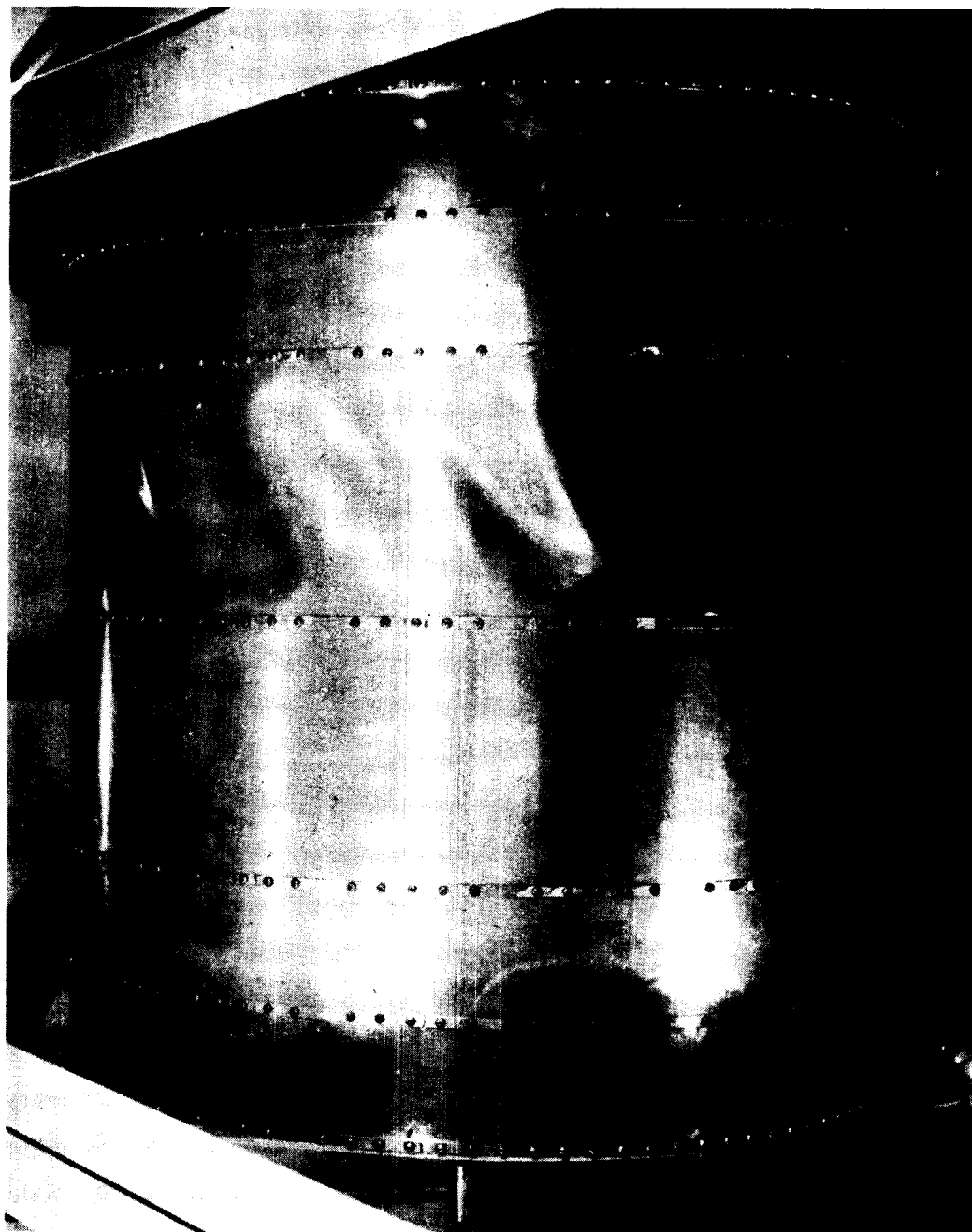
Figure 10. — Failure of specimen No. 13A.
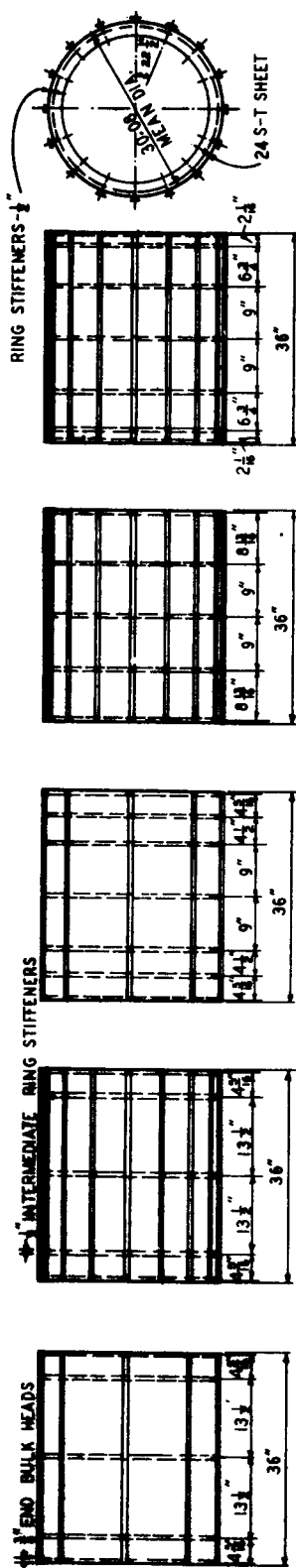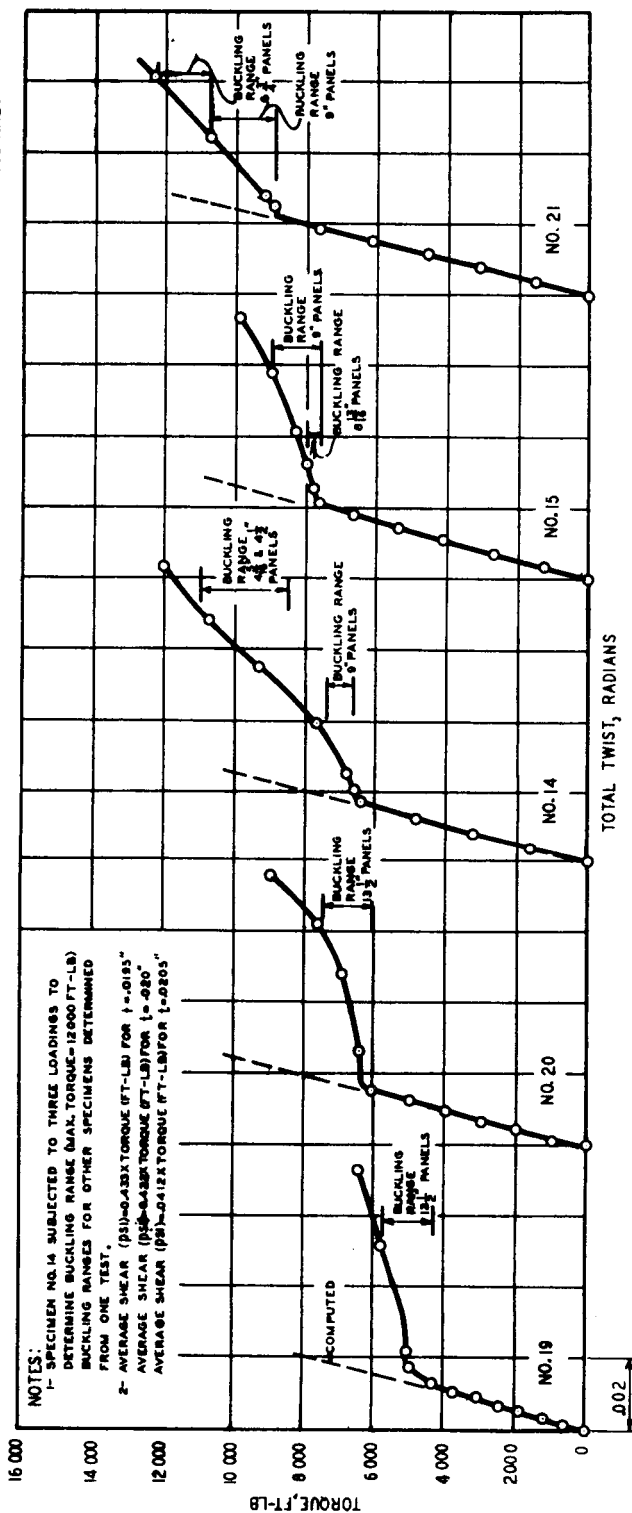
Figure 11.- SHEAR-BUCKLING TORQUES FOR PANELS OF STIFFENED CIRCULAR CYLINDERS
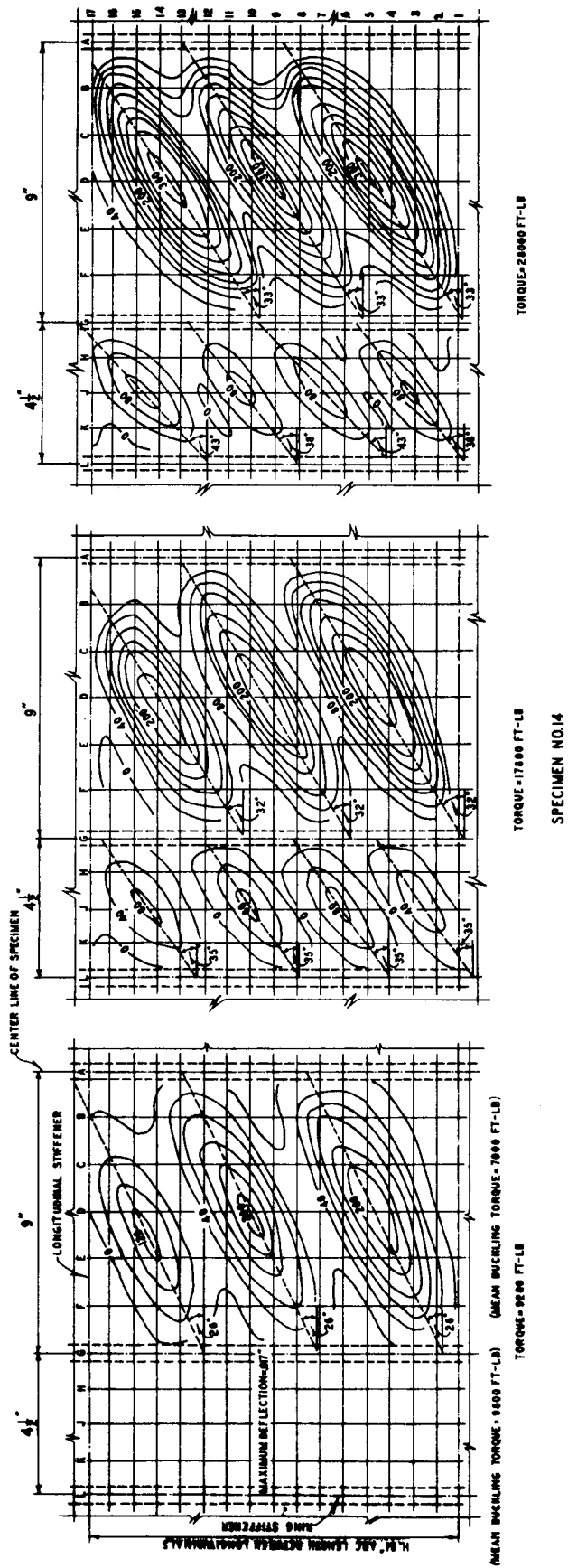
Fig. 12

Figure 12.- DEFLECTION CONTOURS FOR TYPICAL SHEET PANELS
DEVELOPED VIEWS SHOWING RADIAL DEFLECTIONS IN .001 INCHES

SPECIMEN NO.14
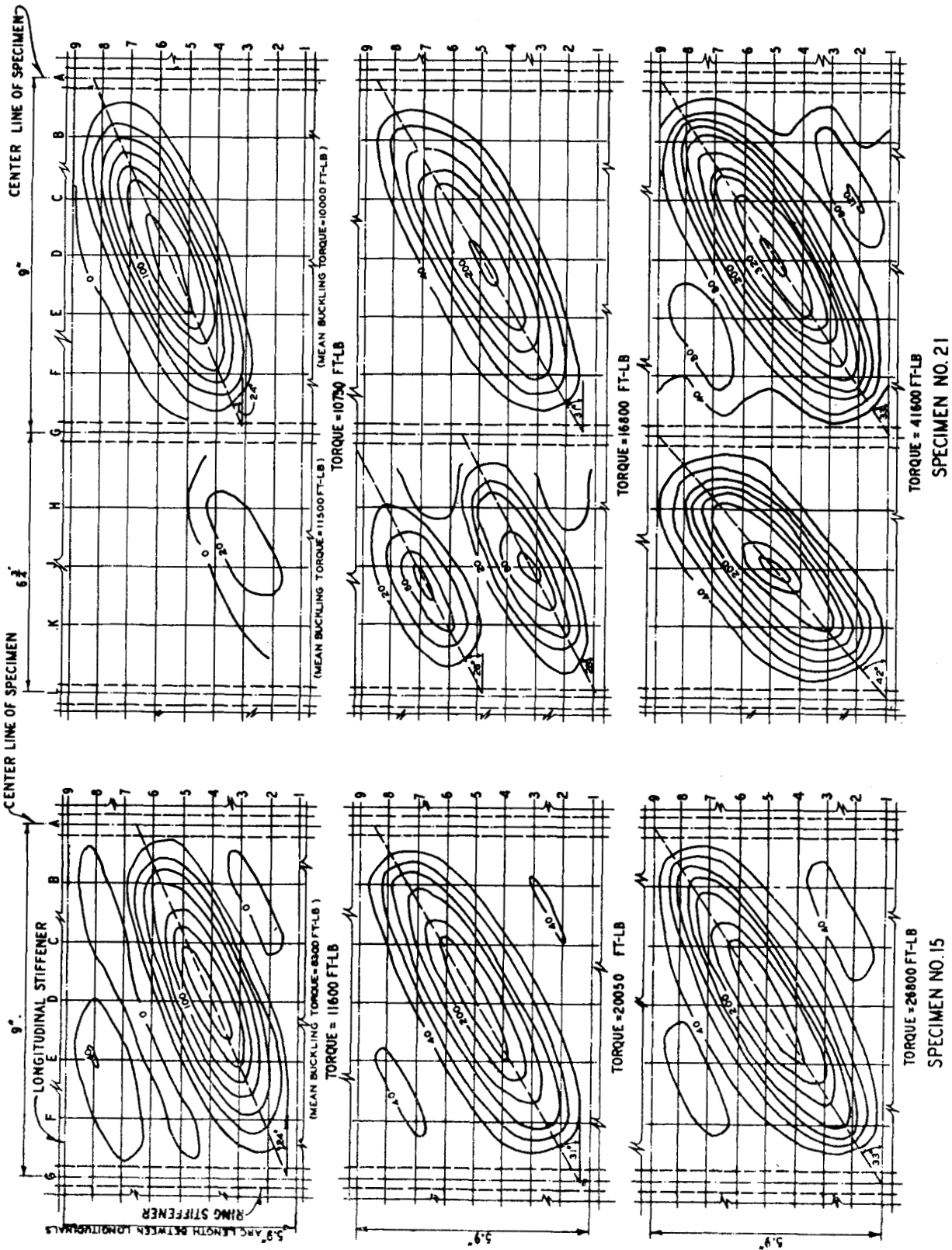
Figure 13.– DEFLECTION CONTOURS FOR TYPICAL SHEET PANELS
DEVELOPED VIEWS SHOWING RADIAL DEFLECTIONS IN .001 IN.

Figure 14.- DEFLECTION CONTOURS FOR TYPICAL SHEET PANELS
DEVELOPED VIEWS SHOWING RADIAL DEFLECTIONS IN .001 IN.

Fig. 15

w - 88
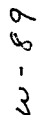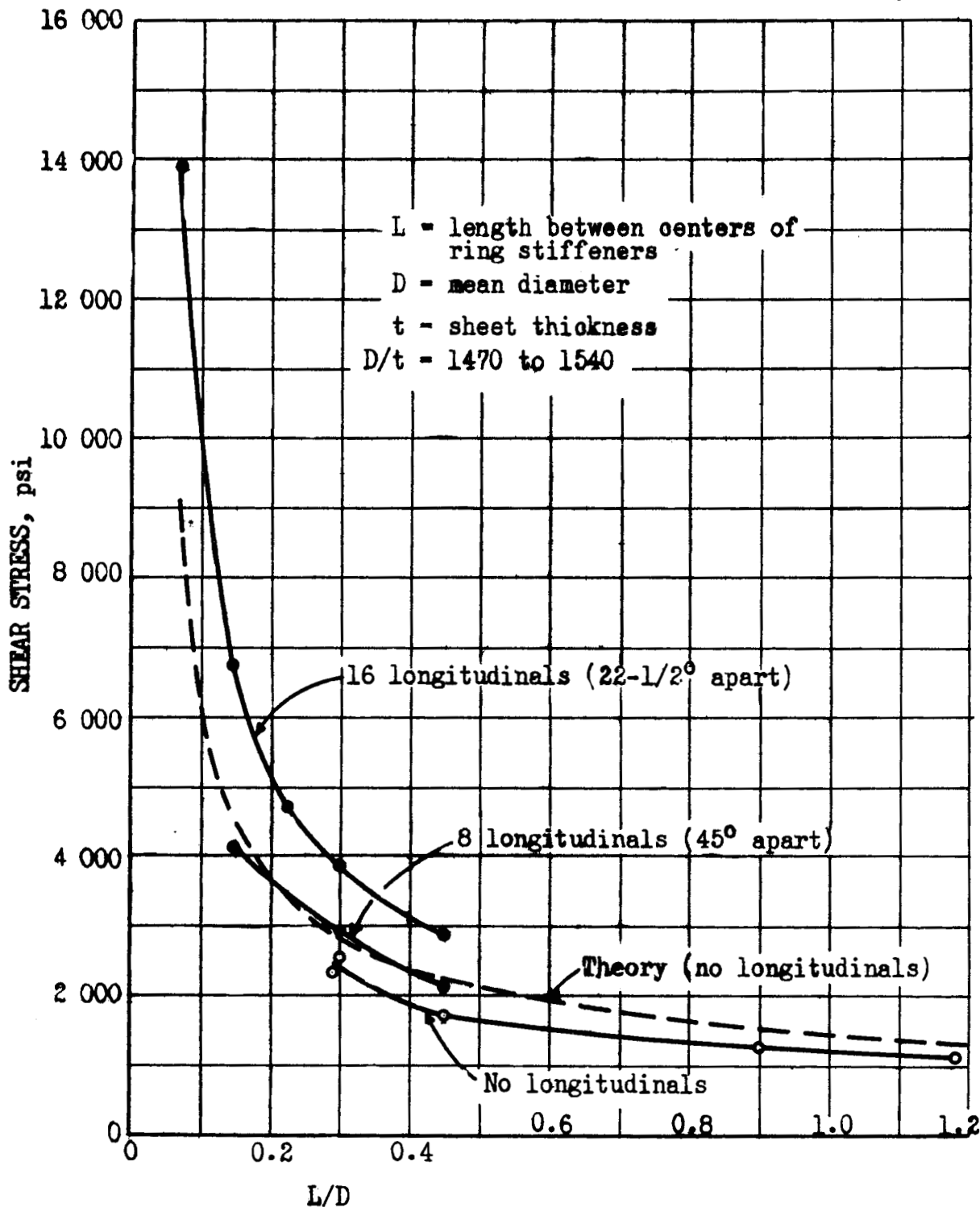
Figure 15.- Shear-Buckling Resistance vs L/D for Different Spacings of Longitudinal Stiffeners
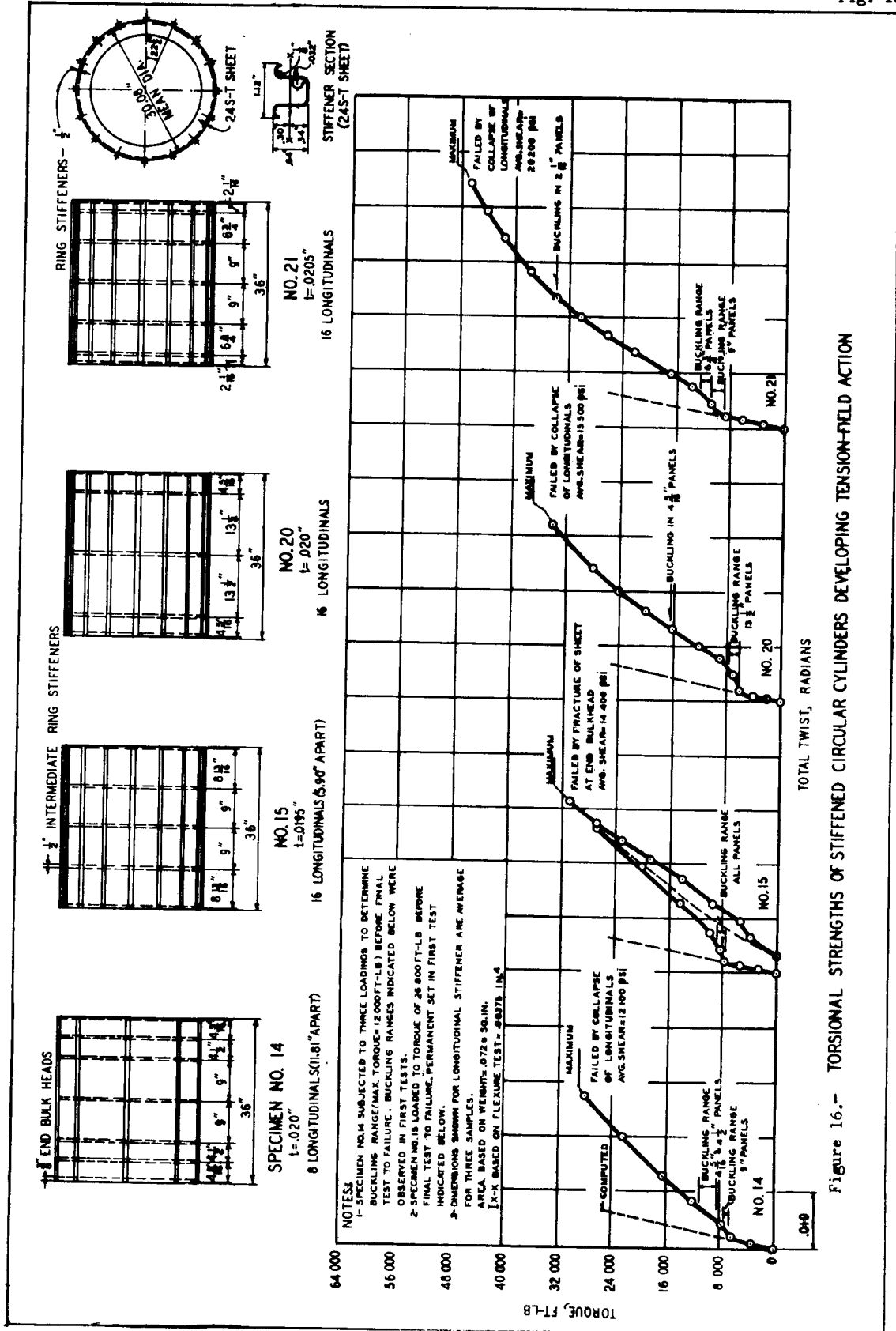
9-6491

24S-T

Figure 16.— TORSIONAL STRENGTHS OF STIFFENED CIRCULAR CYLINDERS DEVELOPING TENSION-FIELD ACTION
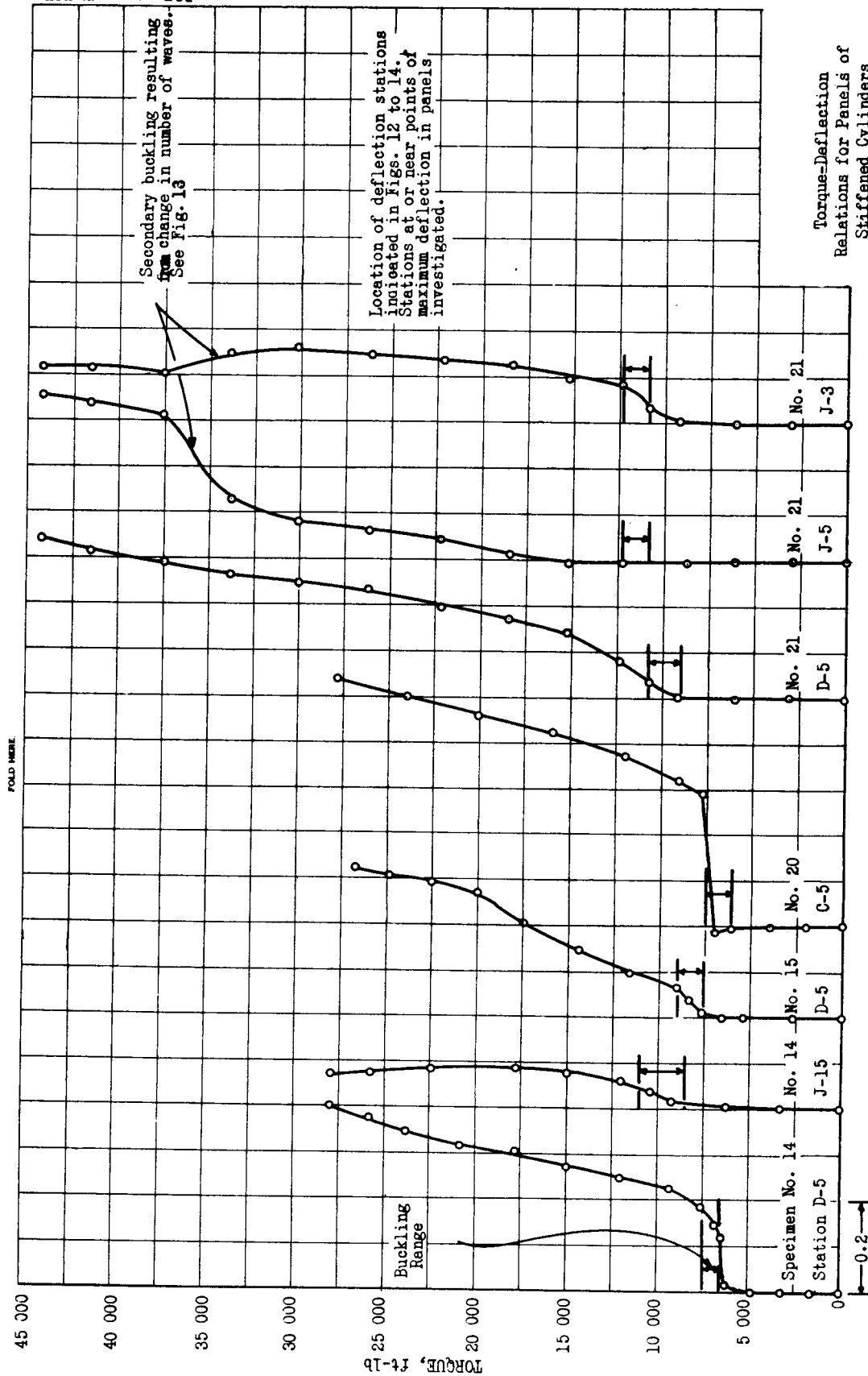
Fig. 17

Figure 17.

Torque-Deflection
Relations for Panels of
Stiffened Cylinders
9-6491
24S-T

Fig. 18

Figure 18.

PRINCIPAL STRESSES FROM STRAIN ROSETTES, psi
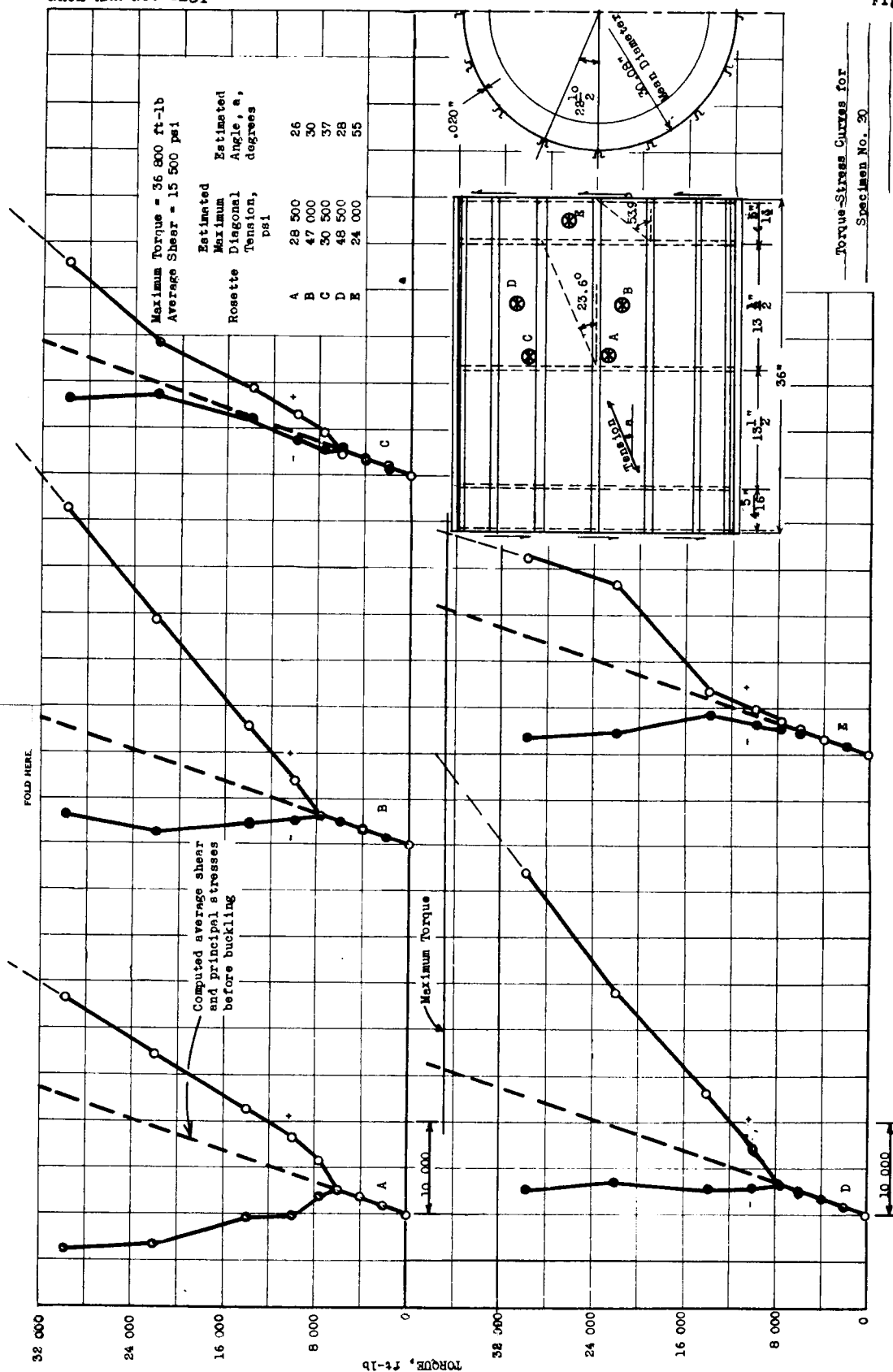
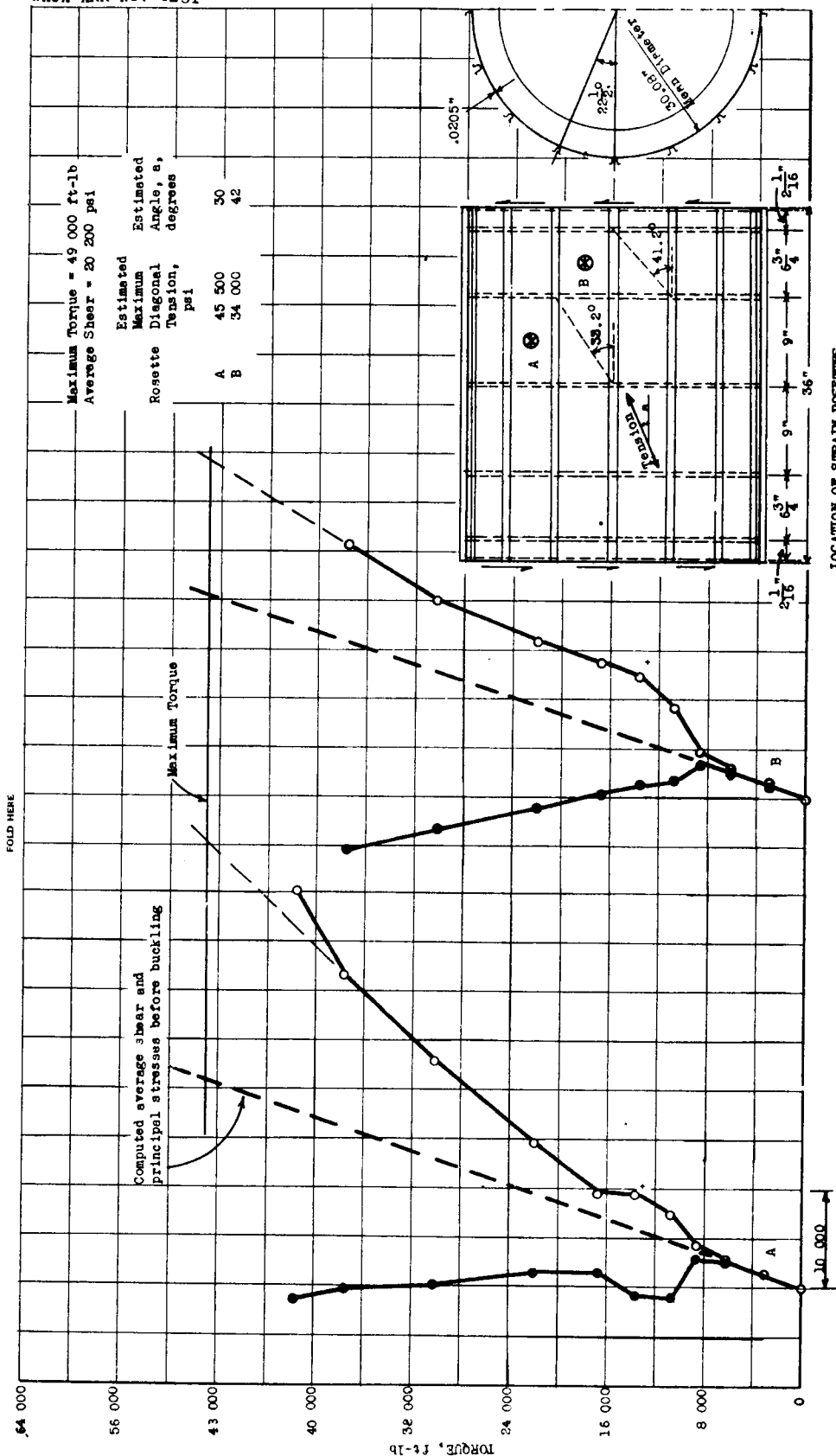Torque-Stress Curves for
Specimen No. 14

9-6491
24S-T

Fig. 19
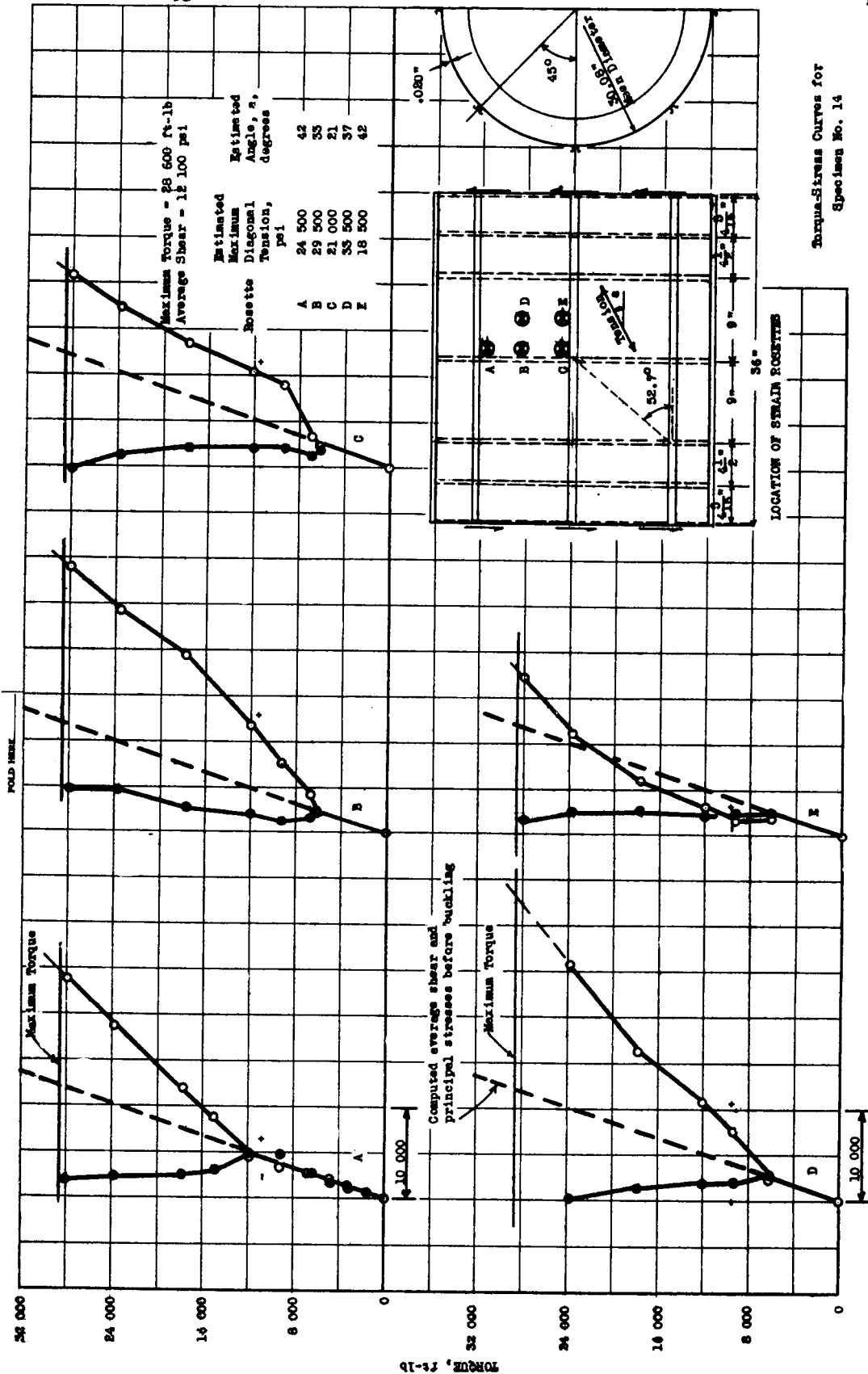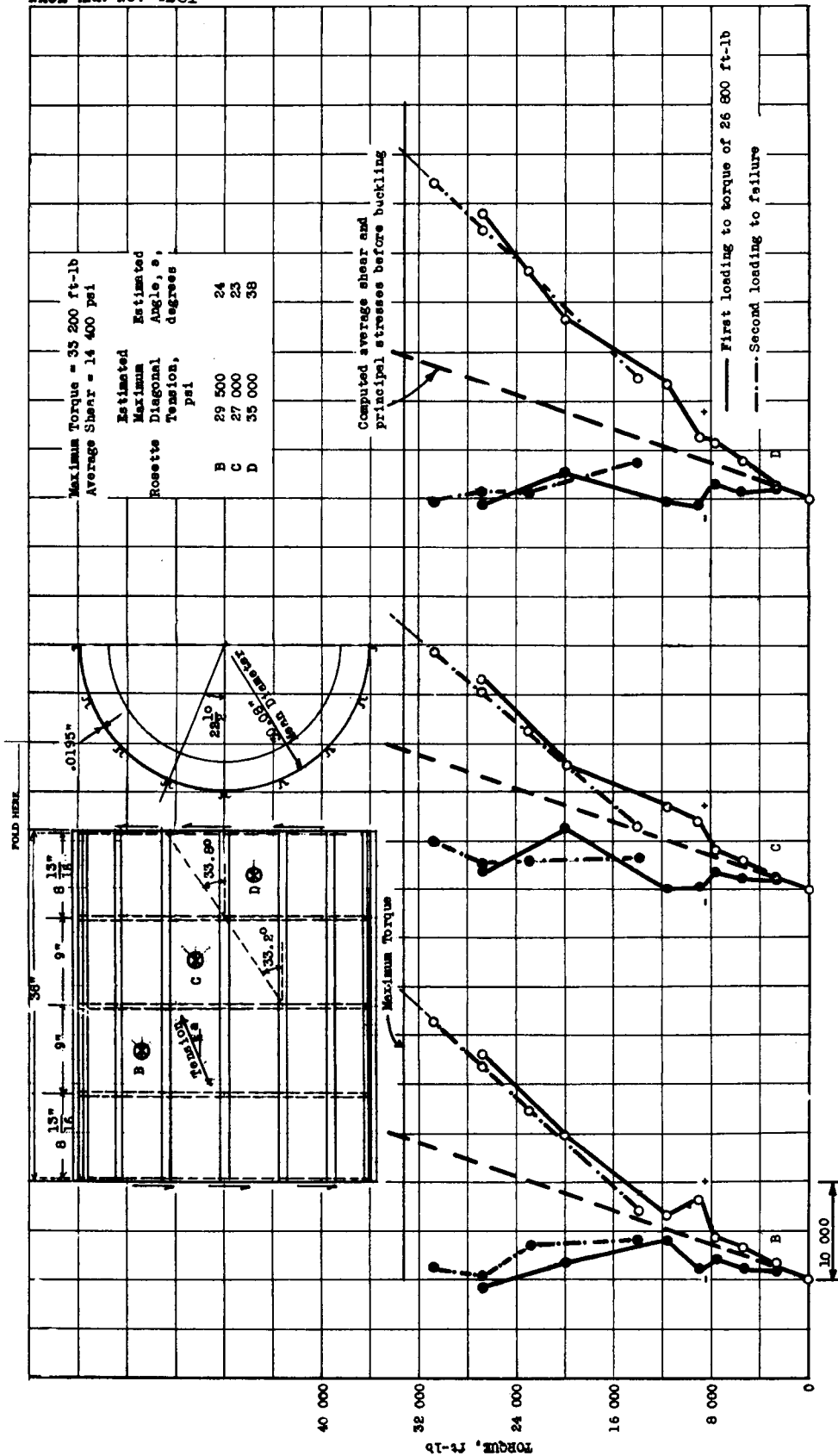
Figure 19.

Torque-Stress Curves for
Specimen No. 15

9-6491

24S-T

Maximum Torque = 35 200 ft-lb
Average Shear = 14 400 psi

Rosette	Estimated Maximum Diagonal Tension, psi	Estimated Angle, s, degrees
B	29 500	24
C	27 000	23
D	35 000	38

Computed average shear and principal stresses before buckling

—— First loading to torque of 26 800 ft-lb
······ Second loading to failure

PRINCIPAL STRESSES FROM STRAIN ROSETTES, psi

TORQUE, ft-lb

Figure 20.

PRINCIPAL STRESSES FROM STRAIN ROSETTES, psi

Torque-Stress Curves for
Specimen No. 30

9-6491
24S-T

W - 89

Figure 21.

PRINCIPAL STRESSES FROM STRAIN ROSETTES, psi

Torque-Stress Curves for
Specimen No. 21

9-6491
24S-T

Fig. 22

Figure 22. — Stiffener Deflections and Stresses in Specimen No. 14

Deflections shown are average for three stiffeners.
Stresses indicated by Curves A and B are for one stiffener.
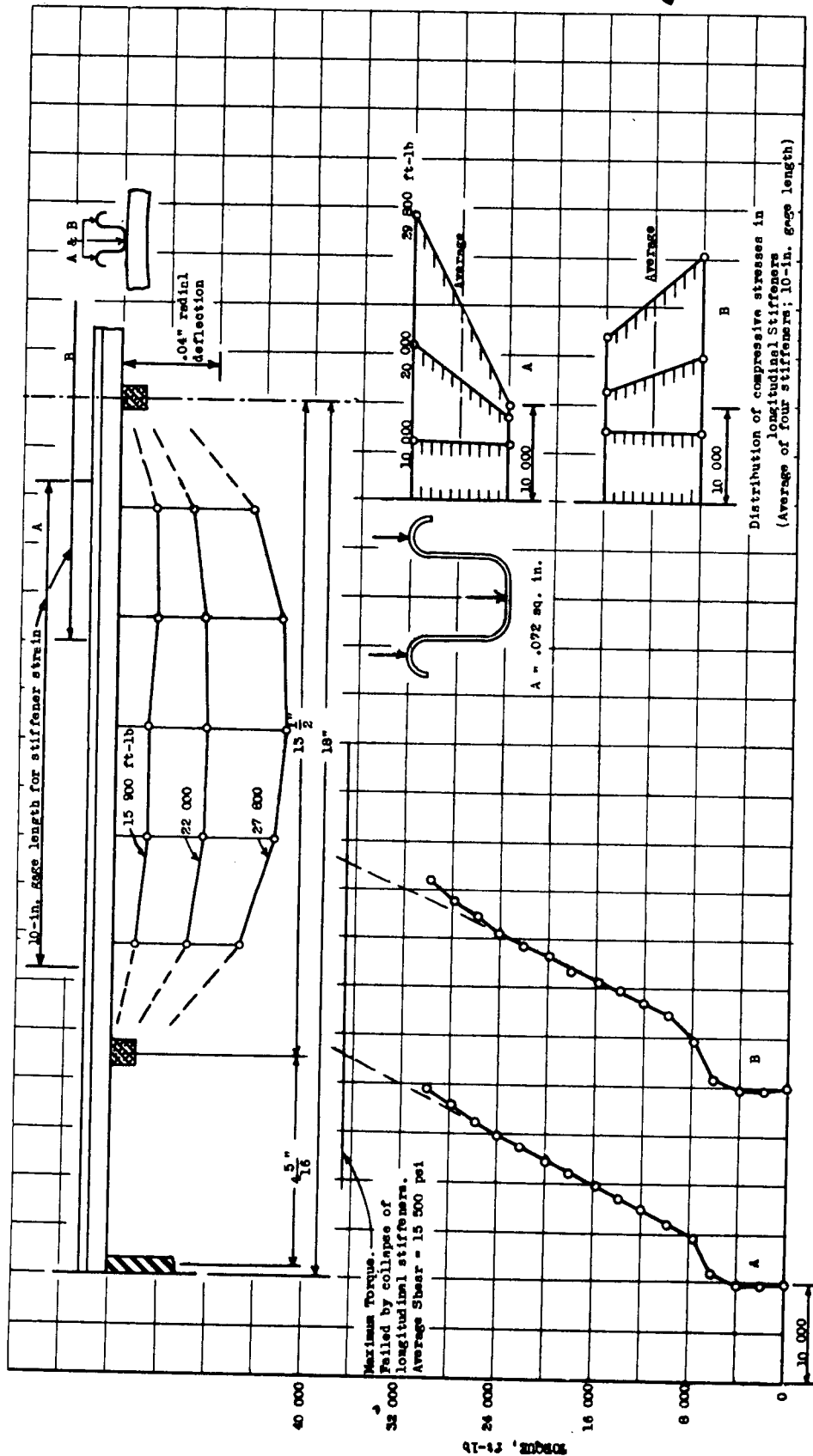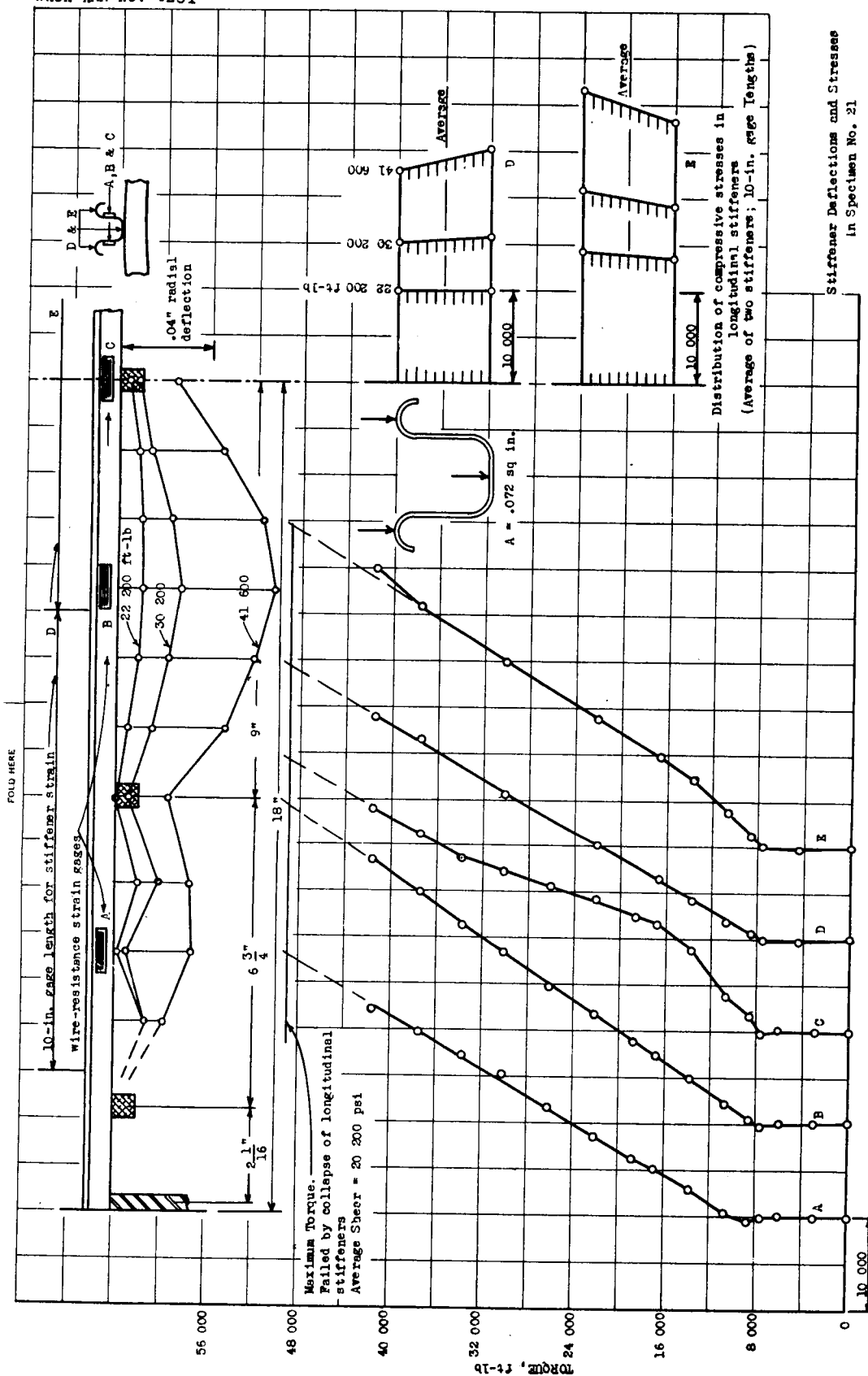Stresses indicated by Curve C are average for two stiffeners.

Fig. 23

W-89

Distribution of compressive stresses in
longitudinal stiffeners
(Average of three stiffeners; 10-in. gage
lengths)
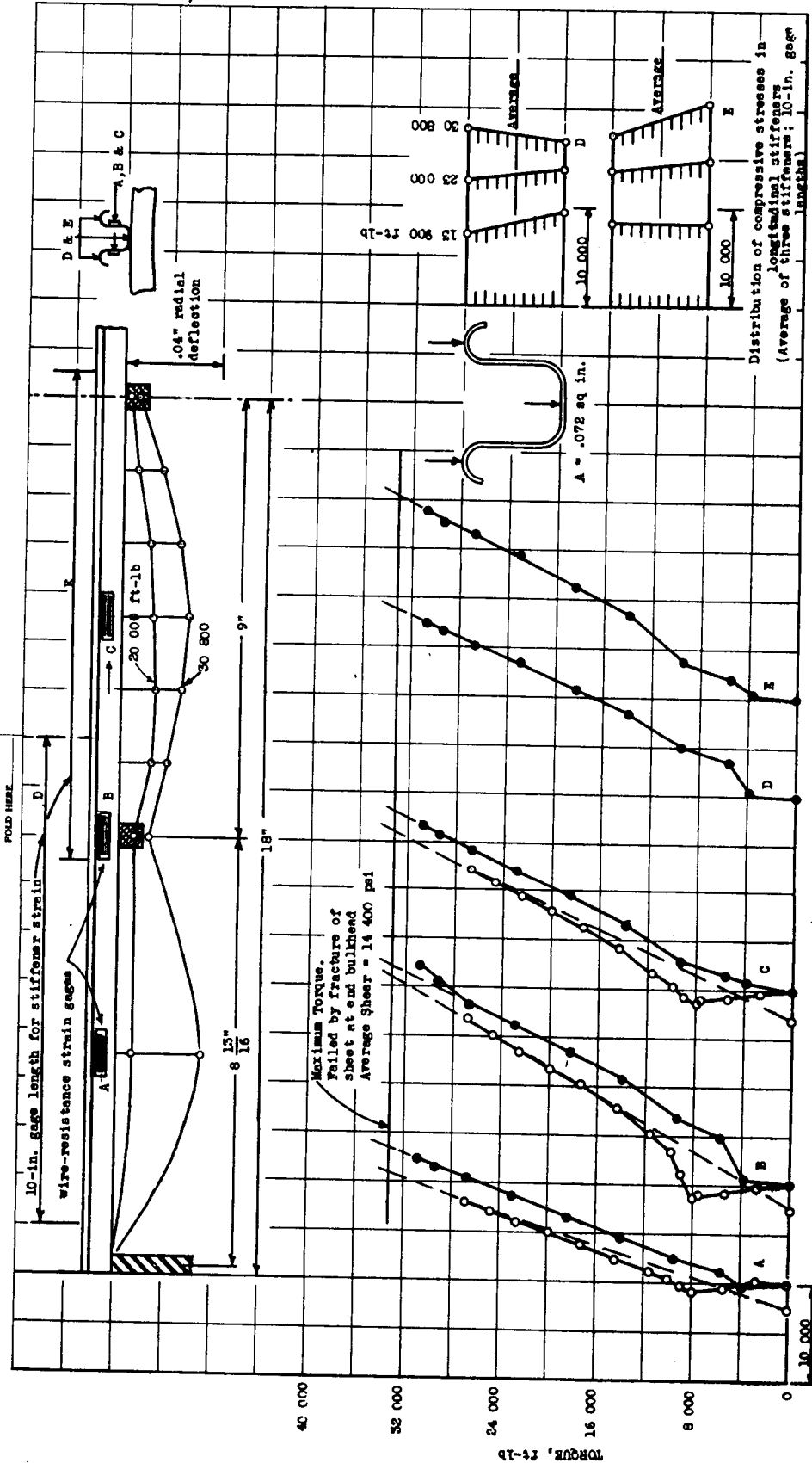
Figure 23.   Stiffener Deflections and Stresses
in Specimen No. 15

9-6491

24S-T

First test to 26 800 ft-lb. ○——
Final test to failure. ●——
Deflections shown are average for three stiffeners.
Stresses indicated by Curves D and E are for three stiffeners.
Stresses indicated by Curves A, B, and C are for one stiffener.

AVERAGE STRESSES, psi

TORQUE, ft-lb

Fig. 24

Figure 24. Stiffener Deflections and Stresses in Specimen No. 20

Deflections shown are average for three stiffeners
Stresses indicated by Curves A and B are for four stiffeners

Figure 25.

AVERAGE STRESSES, psi

Deflections shown are average for three stiffeners.
Stresses indicated by Curves A, B and C are for one stiffener
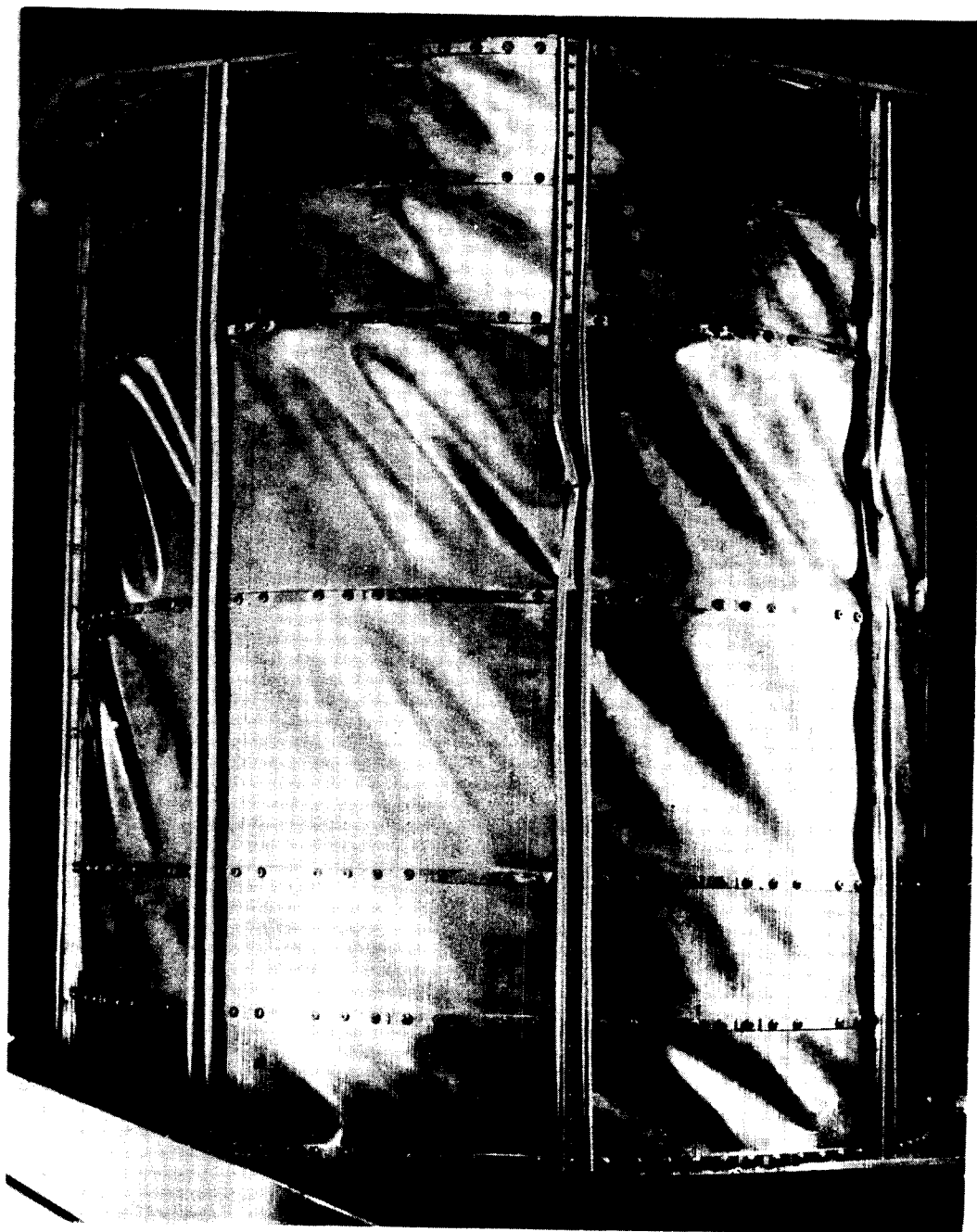Stresses indicated by Curves D and E are for two stiffeners.

Stiffener Deflections and Stresses
in Specimen No. 21

9-6491
24S-T

W-89

Figure 26. — Failure of specimen No. 14.

Figure 27. – Failure of specimen No. 15.

W-89
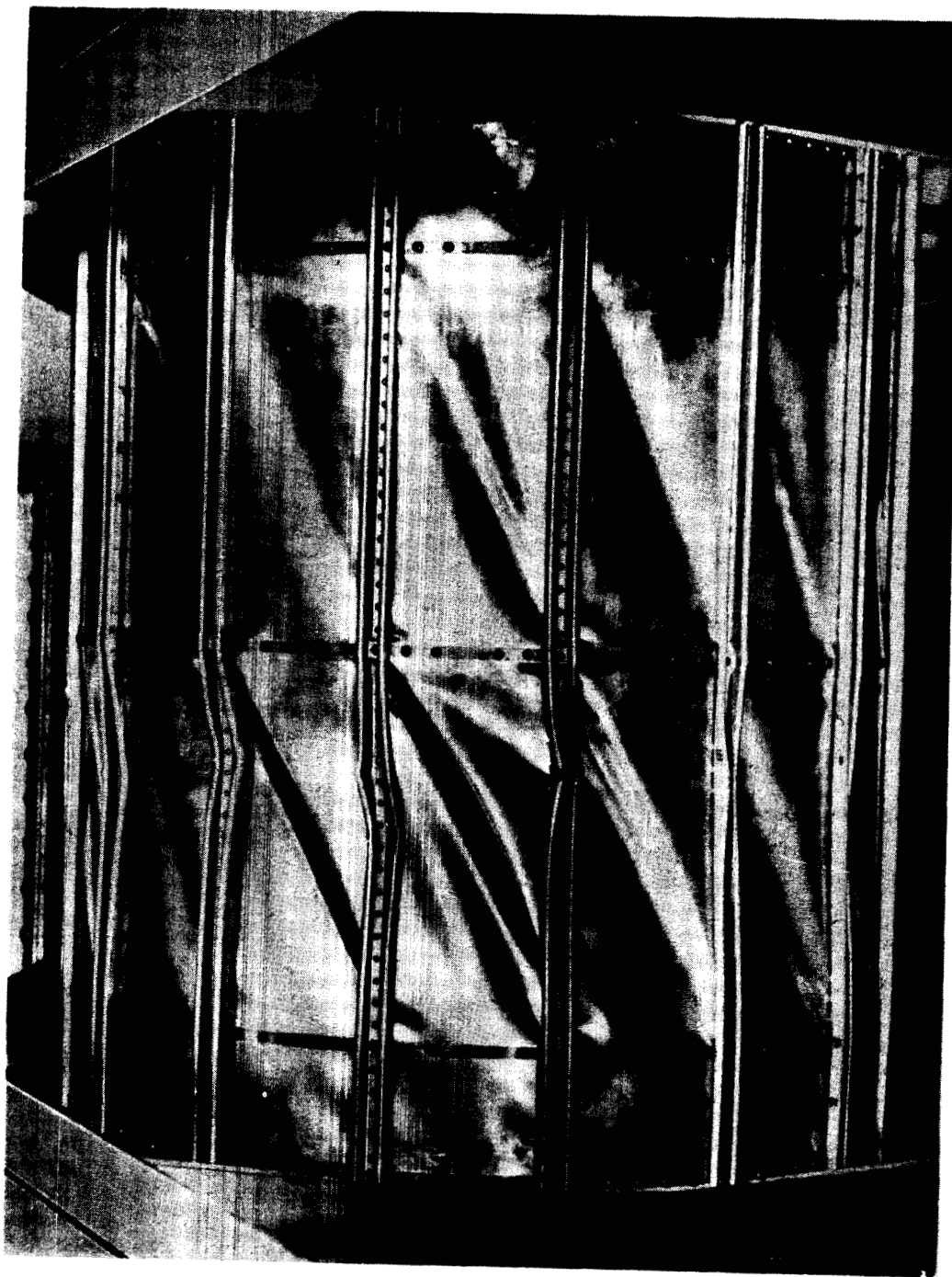
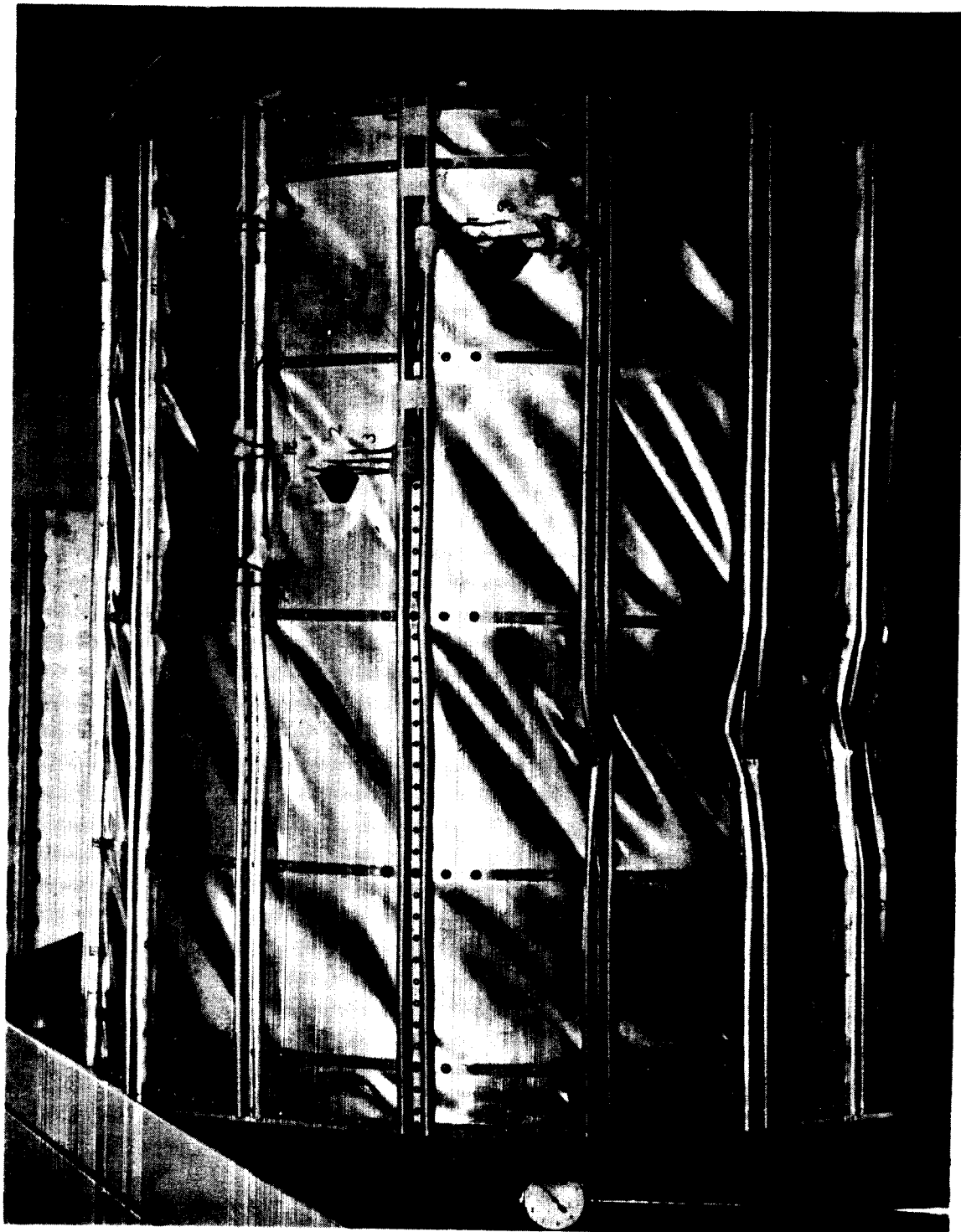Figure 28. — Failure of specimen No. 20.
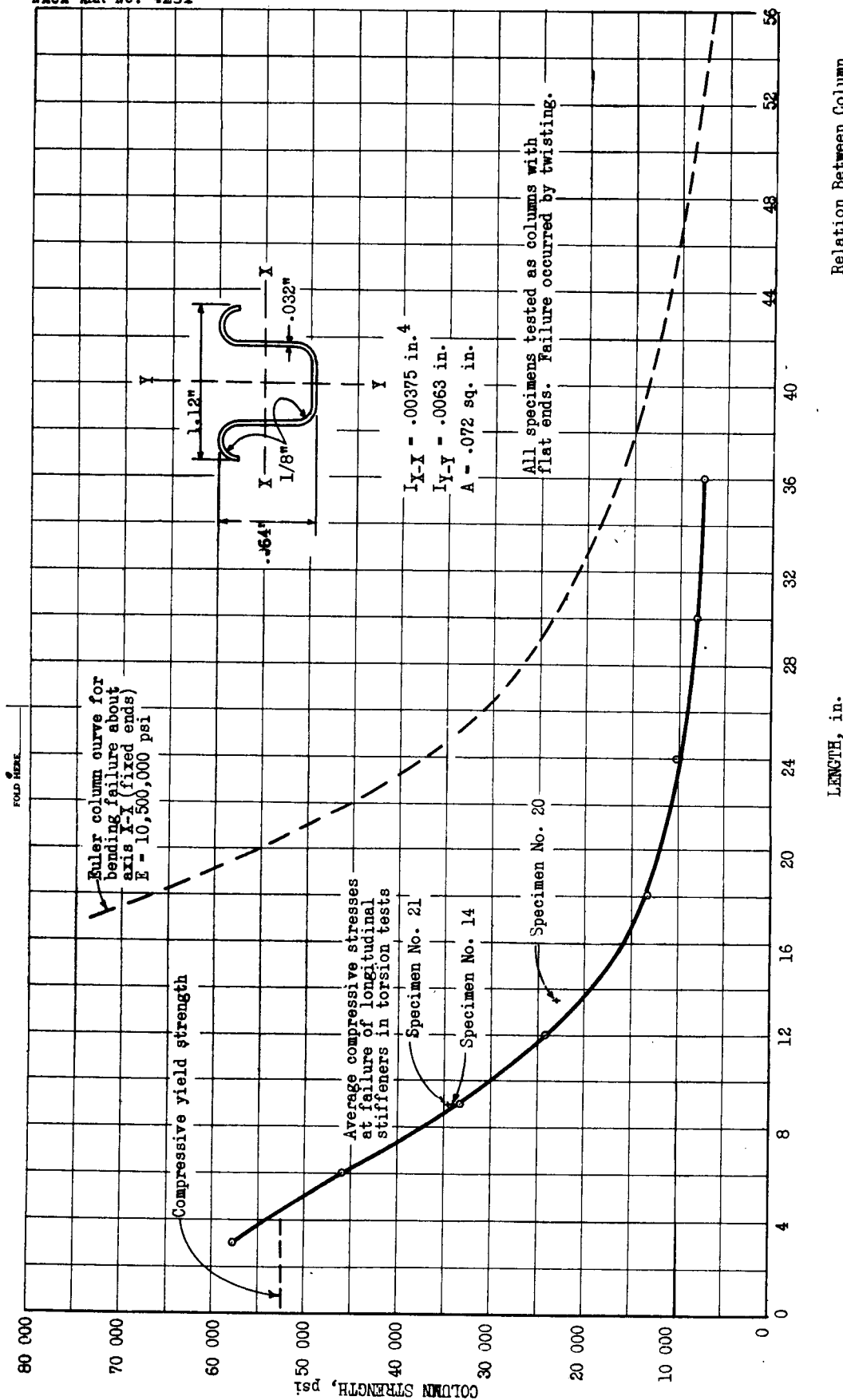
Figure 29. – Failure of specimen No. 21.

Fig. 30

Figure 30.

Relation Between Column
Strength and Length of
Longitudinal Stiffeners
9-6491
24S-T